



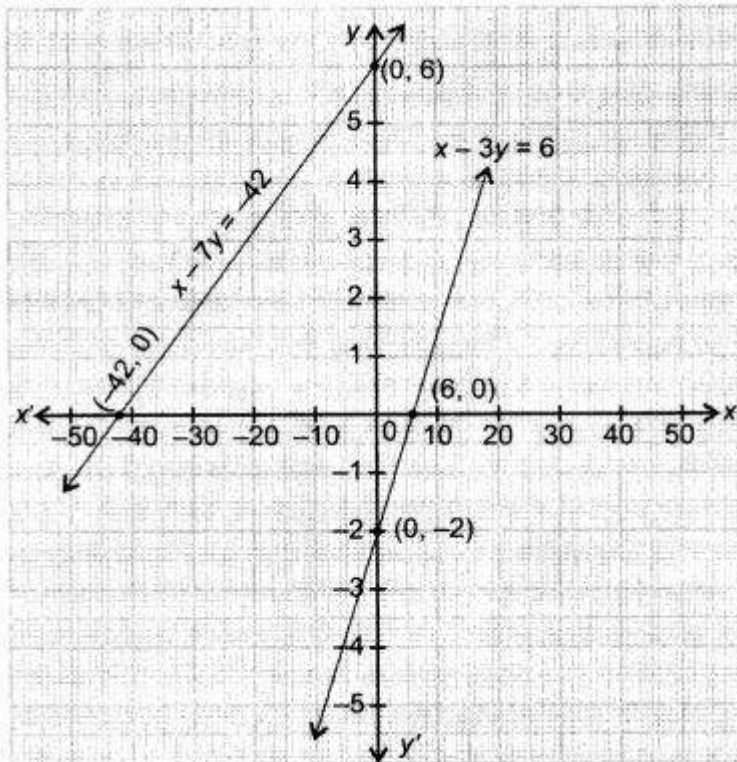
NCERT Solutions of Chapter 3 – Linear Equation In Two Variables

Ex 3.1 Class 10 Question 1.

Aftab tells his daughter, "Seven years ago, I was seven times as old as you were then. Also, three years from now, I shall be three times as old as you will be." (Isn't this interesting)? Represent this situation algebraically and graphically.

Solution:

Let present age of Aftab = x years and present age of Aftab's daughter = y years.



1st Condition :

Seven years ago

$$x - 7 = 7(y - 7)$$

$$\Rightarrow x - 7 = 7y - 49$$

$$\Rightarrow x - 7y = -42$$

Table :

x	0	-42	-35
y	6	0	1

2nd Condition :

Three years later,

$$x + 3 = 3(y + 3)$$

$$x + 3 = 3y + 9$$



$$x - 3y = 6$$

Table :

x	6	0	9
y	0	-2	1

Thus, the algebraic equations are
 $x - 7y + 42 = 0$ and $x - 3y - 6 = 0$

Math Class 10 Ex 3.1 Question 2.

The coach of a cricket team buys 3 bats and 6 balls for ₹ 3900. Later, she buys another bat and 3 more balls of the same kind for ₹ 1300. Represent this situation algebraically and geometrically.

Solution:

Let cost of one bat = ₹ x
and the cost of one ball = ₹ y

A.T.Q.

1st Condition :

$$3x + 6y = 3900$$

Table :

x	0	1300	100
y	650	0	600

2nd Condition :

$$x + 3y = 1300$$

Table :

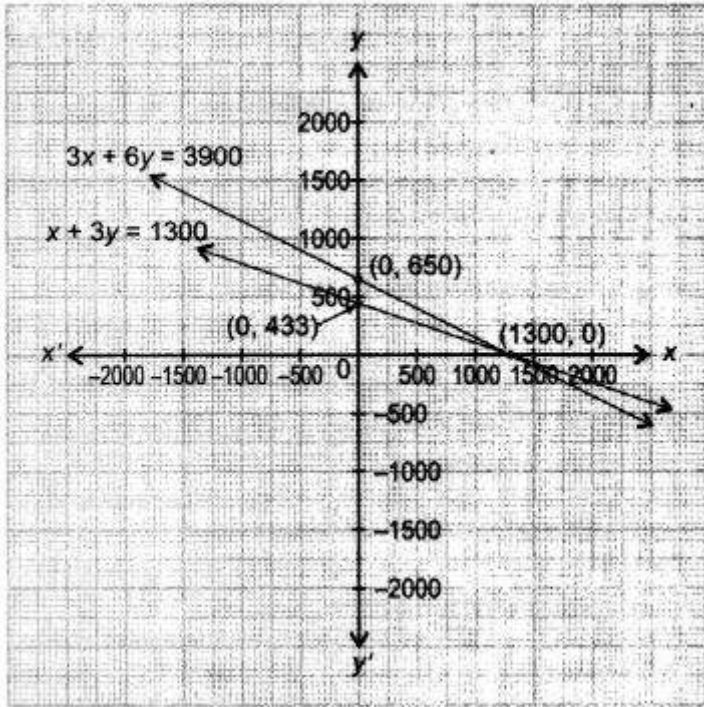
x	0	1300	400
y	433	0	300

Thus, the algebraic equations are $3x + 6y = 3900$





and $x + 3y = 1300$



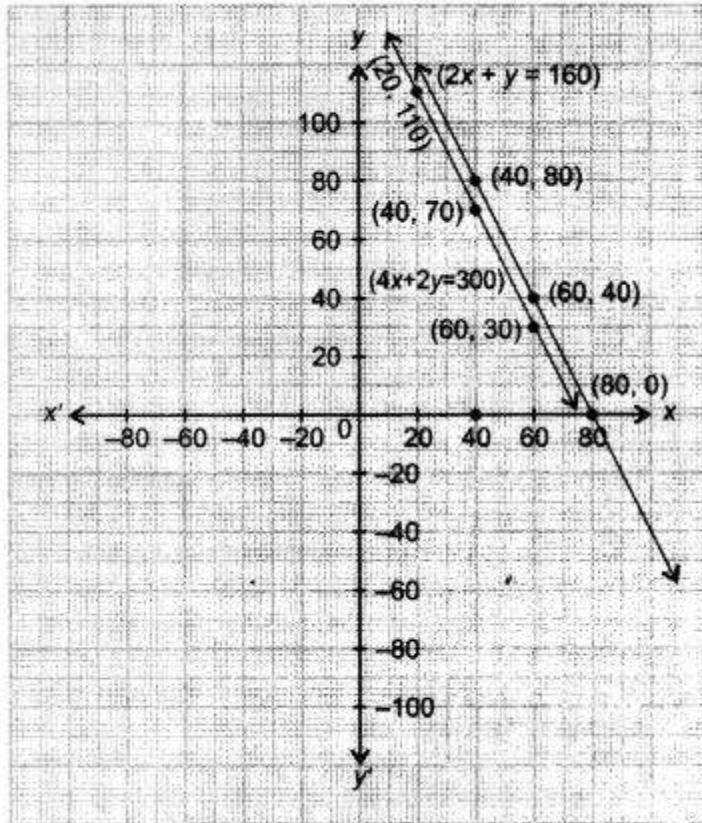
Class 10 Maths Chapter 3 Question 3.

The cost of 2 kg of apples and 1 kg of grapes on a day was found to be ₹ 160. After a month, the cost of 4 kg of apples and 2 kg of grapes is ₹ 300. Represent the situation algebraically and geometrically.

Solution:

Let cost of one kg of apples = ₹ x and the cost of one kg of grapes = ₹ y





A.T.Q.

1st Condition :

$$2x + y = 160$$

Table :

x	80	60	40
y	0	40	80

2nd Condition :

$$4x + 2y = 300$$

Table :

x	60	40	20
y	30	70	110

Thus, algebraic situations are $2x + y = 160$ and $4x + 2y = 300$

Class 10th Exercise 3.2 Question 1.

Form the pair of linear equations in the following problems, and find their solutions graphically.

(i) 10 students of class X took part in a Mathematics quiz. If the number of girls is 4 more than the number of boys, find the number of boys and girls who took part



in the quiz.

(ii) 5 pencils and 7 pens together cost ₹ 50, whereas 7 pencils and 5 pens together cost ₹ 46. Find the cost of one pencil and that of one pen.

Solution:

(i) Let the number of girls be x and number of boys be y .

A.T.Q.

1st Condition :

$$x + y = 10$$

Table :

Table (i)

x	4	6	5
y	6	4	5

2nd Condition :

$$x = y + 4 \Rightarrow x - y = 4$$

Table :

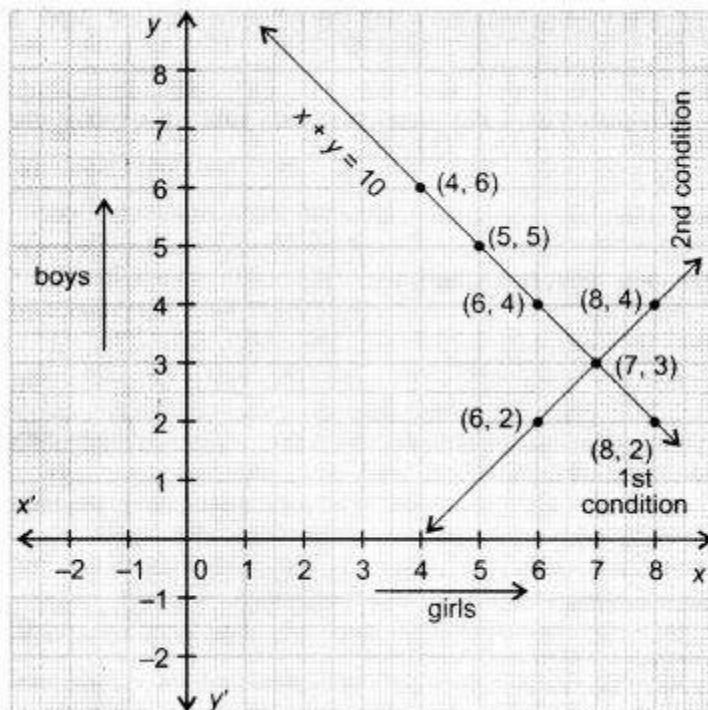
Table (ii)

x	8	6	7
y	4	2	3

Solving

(i) and

(ii) graphically



Both the lines cut at $(7, 3)$



Hence, solutions is (7, 3), i.e. $x = 7, y = 3$
Number of girls – 7 and Number of boys = 3

(ii) Let cost of 1 pencil = ₹ x and cost of 1 pen = ₹ y .

A.T.Q.

1st Condition :

$$5x + 7y = 50$$

Table :

Table (i)

x	3	10	-4
y	5	0	10

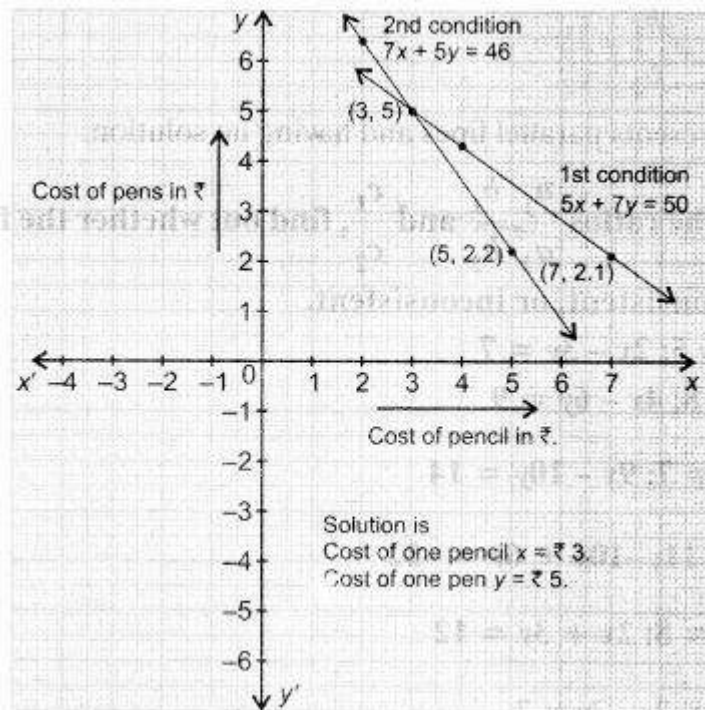
2nd Condition :

$$7x + 5y = 46$$

Table :

Table (ii)

x	3	8	-2
y	5	-2	12



Class 10 Maths Ex 3.2 Question 2.

On comparing the ratios and find out whether the lines representing the following pairs of linear equations intersect at a point, are parallel or coincident:



(i) $5x - 4y + 8 = 7x + 6y - 9 = 0$

(ii) $9x + 3y + 12 = 0, 18x + 6y + 24 = 0$

(iii) $6 - 3y + 10 = 0, 2x - y + 9 = 0$

Solution:

(i) Equations are $5x - 4y + 8 = 7x + 6y - 9 = 0$

Here $\frac{a_1}{a_2} = \frac{5}{7}; \frac{b_1}{b_2} = \frac{-4}{6}; \frac{c_1}{c_2} = \frac{8}{-9}$

$\Rightarrow \frac{a_1}{a_2} \neq \frac{b_1}{b_2}$ as $\frac{5}{7} \neq \frac{-4}{6}$.

\therefore Pair of lines represented by given equations intersect at one point. So, the system has exactly one solution.

(ii) $9x + 3y + 12 = 0, 18x + 6y + 24 = 0$

Here $\frac{a_1}{a_2} = \frac{9}{18} = \frac{1}{2}; \frac{b_1}{b_2} = \frac{3}{6} = \frac{1}{2}; \frac{c_1}{c_2} = \frac{12}{24} = \frac{1}{2}$

Clearly, $\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$

\therefore Pair of equations represents coincident lines and having infinitely many solutions.

(iii) $6x - 3y + 10 = 0, 2x - y + 9 = 0$

Here $\frac{a_1}{a_2} = \frac{6}{2} = 3; \frac{b_1}{b_2} = \frac{-3}{-1} = 3; \frac{c_1}{c_2} = \frac{10}{9}$

Clearly, $\frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$

\therefore It represents parallel lines and having no solution.

Ex 3.2 NCERT Class 10 Question 3.

On comparing the ratios and find out whether the following pair of linear equations are consistent, or inconsistent,

(i) $3x + 2y = 5; 2x - 3y = 7$

(ii) $2x - 3y = 8; 4x - 6y = 9$

(iii) $3/2x + 5/3y = 7; 9x - 10y = 14$



(iv) $5x - 3y = 11$; $-10x + 6y = -22$

(v) $\frac{4}{3}x + 2y = 8$; $2x + 3y = 12$

Solution:

(i) $3x + 2y = 5$, $2x - 3y = 7$

Here $\frac{a_1}{a_2} = \frac{3}{2}$, $\frac{b_1}{b_2} = \frac{2}{-3}$, $\frac{c_1}{c_2} = \frac{-5}{-7} = \frac{5}{7}$

$\therefore \frac{a_1}{a_2} \neq \frac{b_1}{b_2}$ as $\frac{3}{2} \neq \frac{-2}{3}$

\therefore Pair of equations is consistent with unique solution.

(ii) $2x - 3y = 8$, $4x - 6y = 9$

Here $\frac{a_1}{a_2} = \frac{2}{4} = \frac{1}{2}$, $\frac{b_1}{b_2} = \frac{-3}{-6} = \frac{1}{2}$, $\frac{c_1}{c_2} = \frac{8}{9}$

$\therefore \frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$

\therefore Pair of equations is inconsistent, i.e. having no solution.

(iii) $\frac{3}{2}x + \frac{5}{3}y = 7$, $9x - 10y = 14$

Here $\frac{a_1}{a_2} = \frac{3}{2 \times 9} = \frac{1}{6}$, $\frac{b_1}{b_2} = -\frac{5}{3 \times 10} = -\frac{1}{6}$, $\frac{c_1}{c_2} = \frac{-7}{-14} = \frac{1}{2}$

$\therefore \frac{a_1}{a_2} \neq \frac{b_1}{b_2}$

\therefore Pair of equations is consistent with unique solution.



(iv) $5x - 3y = 11, -10x + 6y = -22$

Here $\frac{a_1}{a_2} = \frac{5}{-10} = \frac{-1}{2}, \frac{b_1}{b_2} = \frac{-3}{6} = \frac{-1}{2}, \frac{c_1}{c_2} = \frac{11}{-22} = \frac{-1}{2}$

$\therefore \frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$

\therefore Pair of equations is consistent with infinitely many solutions.

(v) $\frac{4}{3}x + 2y = 8, 2x + 3y = 12$

Here $\frac{a_1}{a_2} = \frac{4}{3 \times 2} = \frac{2}{3}, \frac{b_1}{b_2} = \frac{2}{3}, \frac{c_1}{c_2} = \frac{-8}{-12} = \frac{2}{3}$

$\therefore \frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$

\therefore Pair of equations is consistent with infinitely many solutions.

Ex 3.2 Class 10 NCERT Solutions Question 4.

Which of the following pairs of linear equations are consistent/inconsistent If consistent, obtain the solution graphically:

(i) $x + y = 5, 2x + 2y = 10$

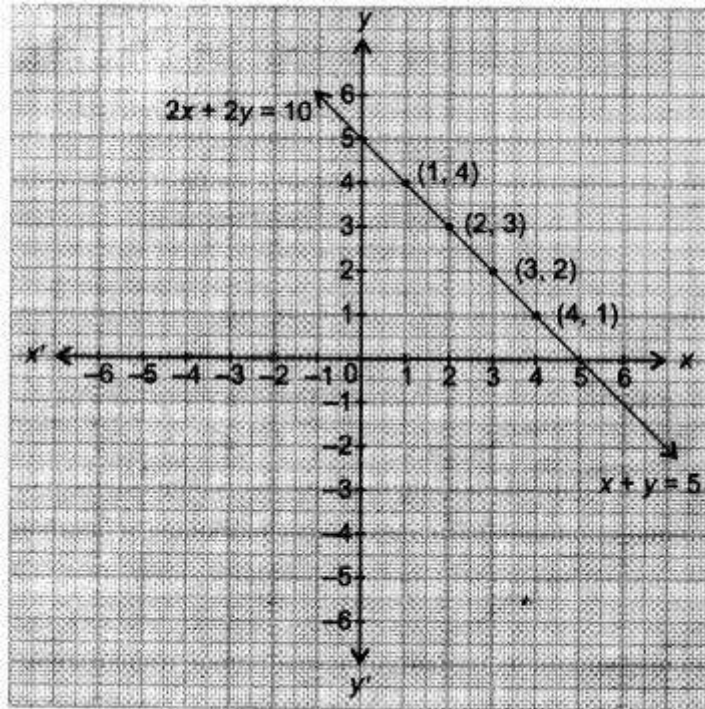
(ii) $x - y = 8, 3x - 3y = 16$

(iii) $2x + y - 6 = 0, 4x - 2y - 4 = 0$

(iv) $2x - 2y - 2 = 0, 4x - 4y - 5 = 0$

Solution:

(i) $x + y = 5, 2x + 2y = 10$



Here,

x	1	4	2	3
y	4	1	3	2

\therefore System of equations is consistent and the graph represents coincident lines.
Table for equation (i),

x	1	4	2	3
y	4	1	3	2

Table for equation (ii),

x	1	4	2	3
y	4	1	3	2



(ii) $x - y = 8$, $3x - 3y = 16$

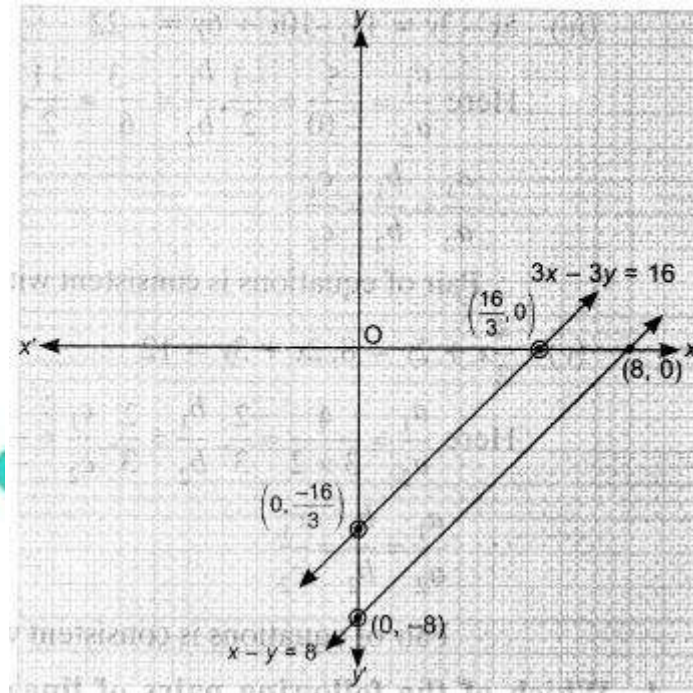
Here $a_1 a_2 \neq 13$,

$$\frac{b_1}{b_2} = \frac{-1}{-3} = \frac{1}{3}$$

$$\frac{c_1}{c_2} = \frac{-8}{-16} = \frac{1}{2}$$

$$\therefore \frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$$

Pair of equations is inconsistent. Hence, lines are parallel and

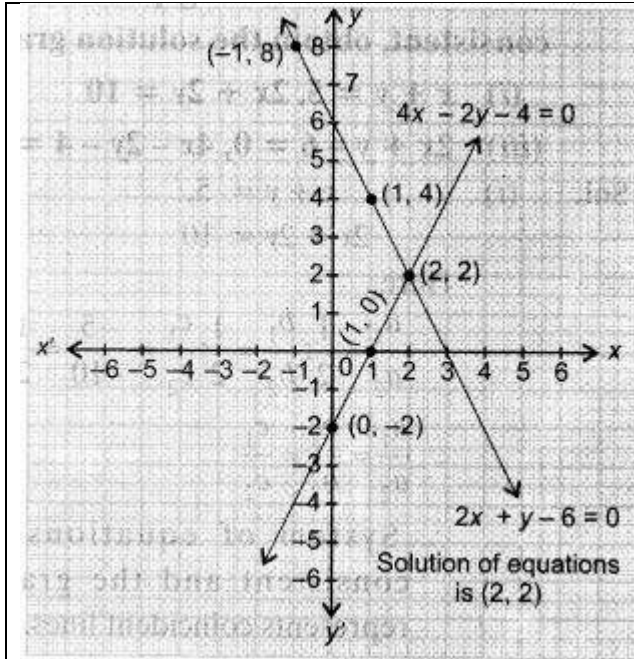


(iii) $2x + y - 6 = 0$, $4x - 2y - 4 = 0$

Here $\frac{a_1}{a_2} = \frac{2}{4} = \frac{1}{2}$, $\frac{b_1}{b_2} = \frac{1}{-2}$, $\frac{c_1}{c_2} = \frac{-6}{-4} = \frac{3}{2}$

$$\therefore \frac{a_1}{a_2} \neq \frac{b_1}{b_2}$$

\therefore Pair of equations is consistent.



Pair of equations is consistent.

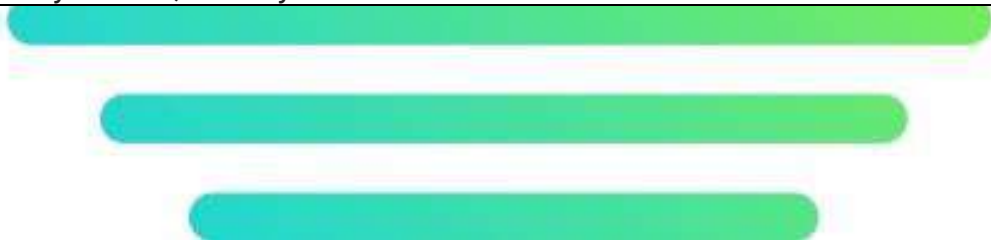
Table for equation $2x + y - 6 = 0$

x	2	1	-1
y	2	4	8

Table for equation $4x - 2y - 4 = 0$

x	1	0	2
y	0	-2	2

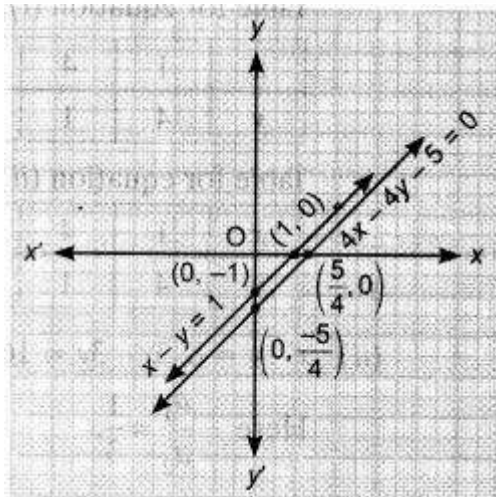
(iv) $2x - 2y - 2 = 0$, $4x - 4y - 5 = 0$





Here $\frac{a_1}{a_2} = \frac{2}{4} = \frac{1}{2}$, $\frac{b_1}{b_2} = \frac{-2}{-4} = \frac{1}{2}$, $\frac{c_1}{c_2} = \frac{-2}{-5} = \frac{2}{5}$

$$\frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$$



\therefore Pair of equations is inconsistent. Hence, lines are parallel and system has no solution.

Class 10 Maths Chapter 3 Exercise 3.2 Question 5.

Half the perimeter of a rectangular garden, whose length is 4 m more than its width, is 36 m. Find the dimensions of the garden.

Solution:

Let length of garden = x m and width of garden = y m

Perimeter of rectangular garden = $2(x + y)$

A.T.Q.

1st Condition :

$$2(x+y) = 36 \Rightarrow x + y = 36$$

2nd Condition :

$$x = y + 4 \Rightarrow x - y = 4 \dots (ii)$$

Adding equation (i) and (ii), we get

$$2x = 40 \Rightarrow x = 20$$

Putting $x = 20$ in equation (i), we get

$$20 + y = 36$$

$$y = 16$$

Hence, dimensions of the garden are 20 m and 16 m.

Exercise 3.2 Class 10 Question 6.

Given the linear equation $2x + 3y - 8 = 0$, write another linear equation in two



variables, such that the geometrical representation of the pair so formed is:

- (i) intersecting lines
- (ii) parallel lines
- (iii) coincident lines

Solution:

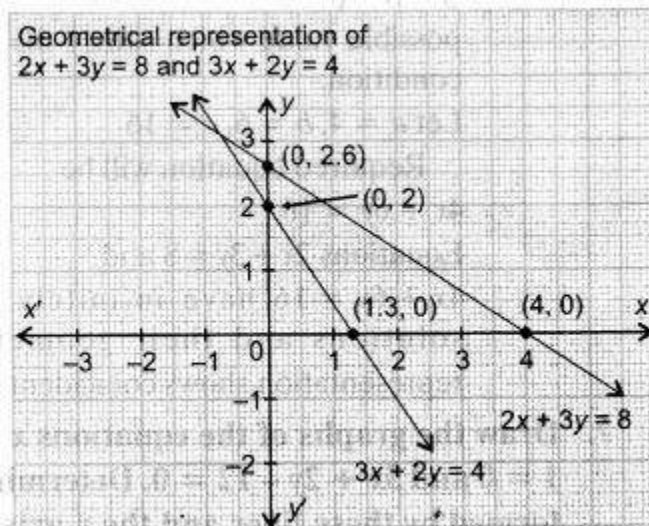
Given equation is $2x + 3y - 8 = 0$

We have $2x + 3y = 8$

Let required equation be $ax + by = c$

Condition :

- (i) For intersecting lines



$2a \neq 3b \neq 8c$ where a, b, c can have any value which satisfy the above condition.

Let $a = 3, b = 2, c = 4$

so, $23 \neq 32 \neq 84$

\therefore Equations are $2x + 3y = 8$ and $3x + 2y = 4$ have unique solution and their geometrical representation shows intersecting lines.

- (ii) Given equation is $2x + 3y = 8$ Required equation be $ax + by = c$

Condition :

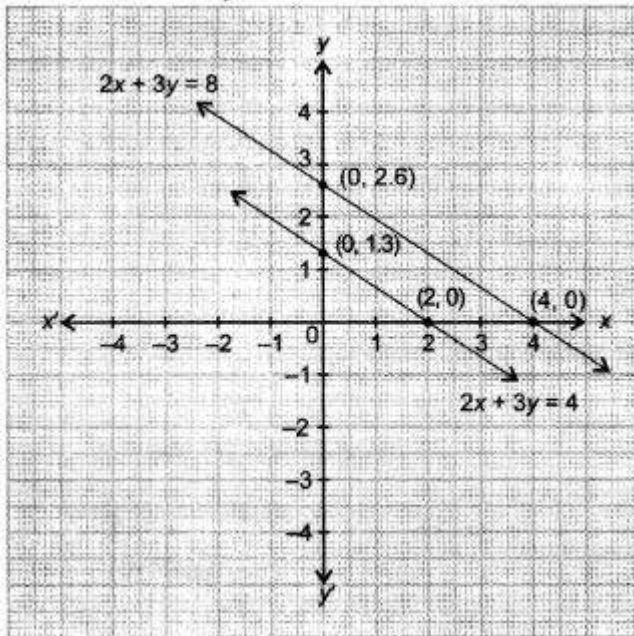
For parallel lines

$2a \neq 3b \neq 8c$

where a, b, c can have any value which satisfy the above condition.

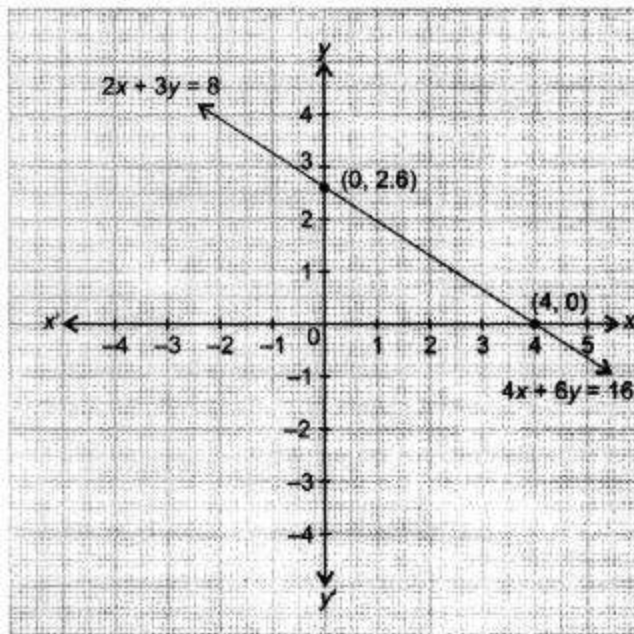
Let, $a = 2, b = 3, c = 4$

Required equation will be $2x + 3y = 4$



Equations $2x + 3y = 8$ and $2x + 3y = 4$ have no solution and their geometrical representation shows parallel lines.

(iii) For coincident lines:



Given equation is $2x + 3y = 8$ Let required equation be $ax + by = c$ For coincident lines.

$2 \times 2 = 3 \times 2 = 8 \times 2$ where a, b, c can have any a, b, c possible value which satisfy the above condition.

Let $a = 4, b = 6, c = 16$ Required equation will be $4x + 6y = 16$.



Equations $2x + 3y = 8$ and $4x + 6y = 16$ have infinitely many solutions and their geometrical representation shows coincident lines.

NCERT Ex 3.2 Class 10 Question 7.

Draw the graphs of the equations $x - y + 1 = 0$ and $3x + 2y - 12 = 0$. Determine the coordinates of the vertices of the triangle formed by these lines and the x - axis, and shade the triangular region.

Solution:

First equation is $x - y + 1 = 0$.

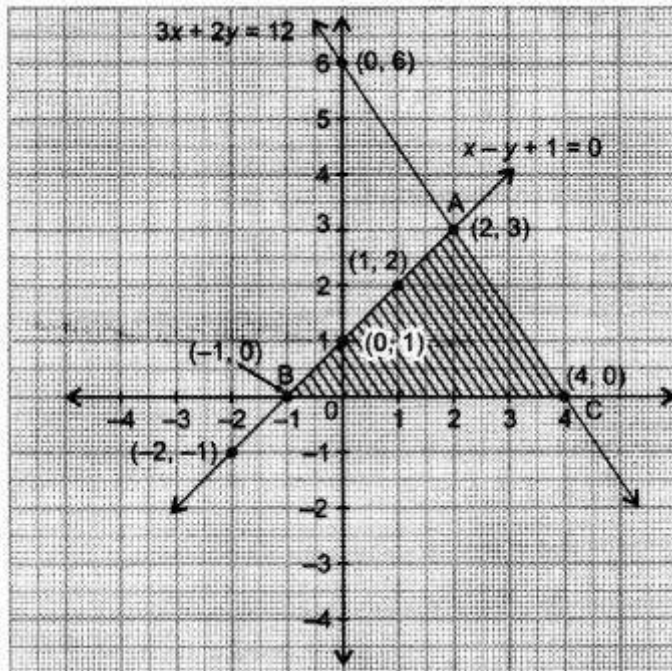
Table for 1st equation $x = y - 1$

x	0	1	-2	2
y	1	2	-1	3

Second equation is $3x + 2y = 12$

x	4	2	0
y	0	3	6

$\Rightarrow 3x = 12 - 2y \Rightarrow x = X=12-2y3$



Required triangle is ABC. Coordinates of its vertices are A(2, 3), B(-1, 0), C(4, 0).

Ex 3.3

Question 1.

Solve the following pair of linear equations by the substitution method,

(i) $x + y = 14, x - y = 4$

(ii) $s - t = 3, s/3 + t/2 = 6$



(iii) $3x - y = 3, 9x - 3y = 9$

(iv) $0.2x + 0.3y = 1.3, 0.4x + 0.5y = 2.3$

(v) $\sqrt{2}x + \sqrt{3}y = 0, \sqrt{3}x - \sqrt{8}y = 0$

(vi) $\frac{3x}{2} - \frac{5y}{3} = -2, \frac{x}{3} + \frac{y}{2} = \frac{13}{6}$

Solution:

From equation (i),

$$x + y - 14 \Rightarrow y = 14 - x$$

Putting the value of y in equation (ii), we get

$$x - (14 - x) = 4 \Rightarrow x - 14 + x = 4 \Rightarrow 2x = 4 + 14$$

$$2x = 18 \Rightarrow x = 9$$

Now, putting $x = 9$ in equation (i), we have

$$9 + y = 14 \Rightarrow y = 14 - 9 \Rightarrow y = 5$$

so, $x = 9, y = 5$

(ii) $s - t = 3$

$$\frac{s}{3} + \frac{t}{2} = 6$$

... (i)

... (ii)

From equation (i), $s - t = 3 \Rightarrow s = 3 + t$

Putting the value of s in equation (ii), we get

$$\frac{3+t}{3} + \frac{t}{2} = 6 \Rightarrow \frac{2(3+t) + 3t}{6} = 6$$

$$\Rightarrow 6 + 2t + 3t = 36 \Rightarrow 5t = 36 - 6$$

$$5t = 30 \Rightarrow t = 6$$

Putting $t = 6$ in equation (i), we have

$$s = 3 + 6 = 9$$

So, $s = 9, t = 6$

(iii) $3x - y = 3$

$$9x - 3y = 9$$

... (i)

... (ii)

From equation (i), $3x - y = 3 \Rightarrow 3x = 3 + y \Rightarrow x = \frac{3+y}{3}$

Now, putting the value of x in equation (ii), we have

$$9\left(\frac{3+y}{3}\right) - 3y = 9 \Rightarrow 3(3+y) - 3y = 9 \Rightarrow 9 + 3y - 3y = 9$$

$$9 = 9$$

$\therefore y$ can have infinite real values

$\therefore x$ can have infinite real values because $x = \frac{y+3}{3}$



$$(iv) \quad \begin{array}{l} 0.2x + 0.3y = 1.3 \quad \dots(i) \\ 0.4x + 0.5y = 2.3 \quad \dots(ii) \end{array}$$

From equation (i),

$$0.2x + 0.3y = 1.3 \Rightarrow 0.2x = 1.3 - 0.3y \Rightarrow x = \frac{1.3 - 0.3y}{0.2}$$

Putting the value of x in equation (ii), we have

$$\begin{aligned} 0.4\left(\frac{1.3 - 0.3y}{0.2}\right) + 0.5y &= 2.3 & \Rightarrow 2(1.3 - 0.3y) + 0.5y &= 2.3 \\ \Rightarrow 2.6 - 0.6y + 0.5y &= 2.3 & \Rightarrow -0.1y &= 2.3 - 2.6 \\ \Rightarrow -0.1y &= -0.3 & \Rightarrow y &= 3 \end{aligned}$$

Putting $y = 3$ in equation (i), we get

$$\begin{aligned} 0.2x + 0.3(3) &= 1.3 \Rightarrow 0.2x + 0.9 = 1.3 \\ \Rightarrow 0.2x &= 1.3 - 0.9 \Rightarrow 0.2x = 0.4 \Rightarrow x = 2 \end{aligned}$$

So, $x = 2, y = 3$

$$(v) \quad \begin{array}{l} \sqrt{2}x + \sqrt{3}y = 0 \quad \dots(i) \\ \sqrt{3}x - \sqrt{8}y = 0 \quad \dots(ii) \end{array}$$





From equation (i), we have

$$x = \frac{-\sqrt{3}}{\sqrt{2}}y \quad \dots (iii)$$

Putting this value in equation (ii), we get

$$\sqrt{3}\left(\frac{-\sqrt{3}}{\sqrt{2}}y\right) - \sqrt{8}y = 0 \Rightarrow \frac{-3}{\sqrt{2}}y - \sqrt{8}y = 0 \Rightarrow y = 0$$

Putting $y = 0$ in equation (iii), we have $x = 0$

So, $x = 0, y = 0$

(vi) $\frac{3}{2}x - \frac{5}{3}y = -2 \quad \dots (i)$

$\frac{x}{3} + \frac{y}{2} = \frac{13}{6} \quad \dots (ii)$

From equation (i), we have

$$\frac{3}{2}x = -2 + \frac{5}{3}y \Rightarrow \frac{3}{2}x = \frac{-6 + 5y}{3}$$

$$\Rightarrow x = \frac{2(-6 + 5y)}{9}$$

Putting this value in equation (ii), we have

$$\frac{1}{3}\left[\frac{-12 + 10y}{9}\right] + \frac{y}{2} = \frac{13}{6} \Rightarrow \frac{-12 + 10y}{27} + \frac{y}{2} = \frac{13}{6}$$

$$\Rightarrow \frac{-12 + 10y}{27} - \frac{13}{6} = \frac{-y}{2} \Rightarrow \frac{-24 + 20y - 117}{54} = \frac{-y}{2}$$

$$\Rightarrow \frac{-141 + 20y}{54} = \frac{-y}{2} \Rightarrow -141 + 20y = -27y$$

$$\Rightarrow -141 = -47y \Rightarrow y = 3$$

Now, putting $y = 3$ in equation (i), we have

$$\frac{3}{2}x - \frac{5}{3}(3) = -2 \Rightarrow \frac{3}{2}x - 5 = -2 \Rightarrow \frac{3}{2}x = 3 \Rightarrow x = 2$$

So, $x = 2, y = 3$

Question 2.

Solve $2x + 3y = 11$ and $2x - 4y = -24$ and hence find the value of 'm' for which $y = mx + 3$.

Solution:

Equations are $2x + 3y = 11$

and $2x - 4y = -24$

From equation (i)

$$2x = 11 - 3y$$

Putting this value in equation (ii), we get



$$11 - 3y - 4y = -24 \Rightarrow 11 - 7y = -24 \Rightarrow -7y = -35$$

$$y = 357 \Rightarrow y = 5$$

Putting $y = 5$ in equation (i). we have

$$2x + 3 \times 5 = 11 \Rightarrow 2x + 15 = 11 \Rightarrow 2x = 11 - 15 \Rightarrow 2x = -4 \Rightarrow x = -2$$

Now, putting the value of x and y in equation

$$y = mx + 3 \Rightarrow 5 = -2m + 3 \Rightarrow 2 = -2m \Rightarrow m = -1$$

Question 3.

Form the pair of linear equations for the following problems and find their solution by substitution method.

(i) The difference between two numbers is 26 and one number is three times the other. Find them.

(ii) The larger of two supplementary angles exceeds the smaller by 18 degrees. Find them.

(iii) The coach of a cricket team buys 7 bats and 6 balls for ₹ 3800. Later, she buys 3 bats and 5 balls for ₹ 1750. Find the cost of each bat and each ball,

(iv) The taxi charges in a city consist of a fixed charge together with the charge for the distance covered. For a distance of 10 km, the charge paid is ₹ 105 and for a journey of 15 km, the charge paid is ₹ 155. What are the fixed charges and the charge per km? How much does a person have to pay for travelling a distance of 25 km?

(v) A fraction becomes $\frac{9}{2}$, if 2 is added to both the numerator and the denominator. If, 3 is added to both the numerator and denominator it becomes $\frac{5}{6}$, Find the fraction.

(vi) Five years hence, the age of Jacob will be three times that of his son. Five years ago, Jacob's age was seven times that of his son. What are their present ages?

Solution:

(i) Let 1st number be x and 2nd number be y .

Let $x > y$

1st condition :

$$x - y = 26$$

2nd condition :

$$x = 3y$$

Putting $x = 3y$ in equation (i)

$$3y - y = 26 \Rightarrow 2y = 26 \Rightarrow y = 13$$

From (ii)

$$x = 3 \times 13 = 39$$

\therefore One number is 13 and the other number is 39.

(ii) Let one angle be x and its supplementary angle = y

Let $x > y$

1st Condition :

$$x + y = 180^\circ$$

**2nd Condition :**

$$x - y = 18^\circ \Rightarrow x = 18^\circ + y$$

From equation (ii), putting the value of x in equation (i),

$$18^\circ + y + y = 180^\circ \Rightarrow 18^\circ + 2y = 180^\circ$$

$$2y = 162^\circ \Rightarrow y = 81^\circ$$

$$\text{From (ii) } x = 18^\circ + 81^\circ = 99^\circ \Rightarrow x = 99^\circ$$

\therefore One angle is 81° and another angle is 99° .

(iii) Let cost of 1 bat = ₹ x and cost of 1 ball = ₹ y

1st Condition:

$$7x + 6y = 3800$$

2nd Condition:

$$3x + 5y = 1750$$

From equation (ii), we get

Putting $x = \frac{1750 - 5y}{3}$ in equation (i), we get

$$7\left[\frac{1750 - 5y}{3}\right] + 6y = 3800 \quad \Rightarrow \quad \frac{12250 - 35y}{3} + 6y = 3800$$

$$\Rightarrow 12250 - 35y + 18y = 11400$$

$$\Rightarrow 12250 - 17y = 11400$$

$$\Rightarrow -17y = 11400 - 12250$$

$$\Rightarrow -17y = -850$$

$$\Rightarrow \boxed{y = 50}$$

Putting the value of y in equation (i), we have

$$7x + 6 \times 50 = 3800 \Rightarrow 7x = 3800 - 300$$

$$\Rightarrow 7x = 3500 \Rightarrow \boxed{x = 500}$$

\therefore Cost of one bat = ₹ 500 and cost of one ball = ₹ 50.

putting $x = 1750 - 5y/3$ in equation (i), we get

Cost of one bat = ₹ 500 and cost of one ball = ₹ 50.

(iv) Let fixed charges be ₹. v and charge for per km be ₹ y .

A.T.Q.**1st Condition :**

$$x + 10y = 105$$

2nd Condition :

$$x + 15y = 155$$

From equation (i), we get

$$x = 105 - 10y$$

Putting this value in equation (ii), we have

$$105 - 10y + 15y = 155 \Rightarrow 105 + 5y = 155$$

$$\Rightarrow 5y = 155 - 105 \Rightarrow 5y = 50 \Rightarrow y = 10$$

Now, putting $y = 10$ in equation (i), we have



$x + 10(10) = 105 \Rightarrow x + 100 = 105 \Rightarrow x = 5$
Fixed charges is ₹ 5 and charges per km is ₹ 10.

3rd Condition :

For distance of 25 km

$$x + 25y = 5 + 25(10) = 5 + 250 = 255$$

Amount paid for travelling 25 km is ₹ 255.

(v) Let numerator be x and denominator be y .

\therefore Fraction is x/y

A.T.Q.

1st condition :

$$\frac{x+2}{y+2} = \frac{9}{11} \quad \Rightarrow 11x + 22 = 9y + 18$$

$$11x - 9y = 18 - 22 \quad \Rightarrow 11x - 9y = -4 \quad \dots (i)$$

2nd condition :

$$\frac{x+3}{y+3} = \frac{5}{6} \quad \Rightarrow 6x + 18 = 5y + 15 \Rightarrow 6x - 5y = 15 - 18$$

$$\Rightarrow 6x - 5y = -3 \quad \dots (ii)$$

From equation (i), we get

$$11x = 9y - 4 \quad \Rightarrow x = \frac{9y - 4}{11}$$

Putting this value in equation (ii), we have

$$6 \left[\frac{9y - 4}{11} \right] - 5y = -3 \quad \Rightarrow \frac{54y - 24}{11} - 5y = -3$$

$$\Rightarrow 54y - 24 - 55y = -33 \quad \Rightarrow -y = -33 + 24$$

$$\Rightarrow -y = -9 \quad \Rightarrow \boxed{y = 9}$$

Putting the value of y in equation (i), we get

$$\Rightarrow 11x - 9(9) = -4 \quad \Rightarrow 11x - 81 = -4$$

$$\Rightarrow 11x = -4 + 81 \quad \Rightarrow 11x = 77 \quad \Rightarrow \boxed{x = 7}$$

\therefore Fraction is $\frac{x}{y} = \frac{7}{9}$.

(vi) Let present age of Jacob be x years and that of his son be y years.

A.T.Q.

1st Condition :

$$x + 5 = 3(y + 5) \Rightarrow x + 5 = 3y + 15 \Rightarrow x - 3y = 15 - 5 \Rightarrow x - 3y = 10$$

2nd Condition:



$$x - 5 = 7(y - 5) \Rightarrow x - 5 = 7y - 35 \Rightarrow x = 7y - 35 + 5$$
$$\Rightarrow x = 7y - 30$$

Putting the value of 'x' in equation (i), we get

$$7y - 30 - 3y = 10$$

$$4y - 30 = 10$$

$$4y = 40 \Rightarrow y = 10$$

putting the value of y in equation(ii), we get

$$x = 7(10) - 30 = 70 - 30 \Rightarrow x = 40$$

Hence, the present age of Jacob is 40 years and that of his son is 10 years.

Ex 3.4

Question 1.

Solve the following pair of linear equations by the elimination method and the substitution

(i) $x + y = 5$ and $2x - 3y = 4$

(ii) $3x + 4y = 10$ and $2x - 2y = 2$

(iii) $3x - 5y - 4 = 0$ and $9x = 2y + 7$

(iv) $x/2 + 2y/3 = -1$ and $x - y/3 = 3$

Solution:

(i) By Elimination Method:

Equations are $x + y = 5$

and $2x - 3y = 4$

Multiply equation (i) by 2 and subtract equation (ii) from it, we have



$$\begin{array}{r} 2x + 2y = 10 \\ 2x - 3y = 4 \\ \hline - \quad + \quad - \\ \hline 5y = 6 \end{array}$$

$$\Rightarrow y = \frac{6}{5}$$

Putting this value in equation (i), we get

$$x + \frac{6}{5} = 5$$

$$x = 5 - \frac{6}{5} = \frac{25 - 6}{5} \Rightarrow \boxed{x = \frac{19}{5}}$$

By Substitution Method:

Equations are $x + y = 5$... (i)

and $2x - 3y = 4$... (ii)

From equation (i)

$$x = 5 - y$$

Putting this value in equation (ii), we have

$$2(5 - y) - 3y = 4 \Rightarrow 10 - 2y - 3y = 4$$

$$\Rightarrow 10 - 5y = 4 \Rightarrow 6 = 5y \Rightarrow \boxed{y = \frac{6}{5}}$$

Putting the value of y in equation (i), we get

$$x + \frac{6}{5} = 5 \Rightarrow x = 5 - \frac{6}{5} \Rightarrow \boxed{x = \frac{19}{5}}$$

(ii) By Elimination method:

Equations are $3x + 4y = 10$

and $2x - 2y = 2$

Multiplying equation (ii) by 2 and adding to equation (i), we





$$3x + 4y = 10$$

$$4x - 4y = 4$$

$$\hline 7x = 14$$

$$\Rightarrow \boxed{x = 2}$$

Now, putting the value of x in equation (i), we get

$$3(2) + 4y = 10 \quad \Rightarrow 6 + 4y = 10$$

$$\Rightarrow 4y = 4 \quad \Rightarrow \boxed{y = 1}$$

By Substitution Method:

Equations are

$$3x + 4y = 10 \quad \dots (i)$$

$$2x - 2y = 2 \quad \dots (ii)$$

From equation (i)

$$\Rightarrow x = \frac{10 - 4y}{3}$$

Putting this value in equation (ii), we get

$$2x - 2y = 2 \quad \Rightarrow x - y = 1$$

$$\Rightarrow \frac{10 - 4y}{3} - y = 1$$

[on putting the value of x

$$\Rightarrow 10 - 4y - 3y = 3 \quad \Rightarrow 7 = 7y \Rightarrow \boxed{y = 1}$$

Putting $y = 1$ in equation (i), we get

$$3x + 4 \times 1 = 10 \quad \Rightarrow 3x = 6 \Rightarrow \boxed{x = 2}$$

(iii) By Elimination Method:





Equations are

$$3x - 5y = 4$$

...(i)

and $9x - 2y = 7$

...(ii)

Multiplying equation (i) by 3 and subtracting from equation (ii),

$$\begin{array}{r} 9x - 2y = 7 \\ 9x - 15y = 12 \\ \hline - \quad + \quad - \\ \hline 13y = -5 \end{array}$$

$$\Rightarrow \boxed{y = \frac{-5}{13}}$$

Putting this value of y in equation (i), we get

$$3x - 5\left(\frac{-5}{13}\right) = 4 \Rightarrow 3x + \frac{25}{13} = 4 \Rightarrow 3x = 4 - \frac{25}{13} = \frac{52 - 25}{13}$$

$$\Rightarrow 3x = \frac{27}{13} \Rightarrow \boxed{x = \frac{9}{13}}$$

By Substitution Method:

We have $3x - 5y = 4$

...(i)

and $9x - 2y = 7$

...(ii)

From equation (i), $x = \frac{4 + 5y}{3}$

Putting this value in equation (ii), we get

$$9\left[\frac{4 + 5y}{3}\right] - 2y = 7 \Rightarrow 3[4 + 5y] - 2y = 7$$

$$\Rightarrow 12 + 15y - 2y = 7 \Rightarrow 12 + 13y = 7$$

$$\Rightarrow 13y = -5 \Rightarrow \boxed{y = \frac{-5}{13}}$$

Putting this value of y in equation (ii), we get

$$9x - 2\left(\frac{-5}{13}\right) = 7$$

$$9x + \frac{10}{13} = 7$$

$$9x = 7 - \frac{10}{13}$$

$$9x = \frac{81}{13} \Rightarrow \boxed{x = \frac{9}{13}}$$



(iv) By Elimination Method:

1st equation :

$$\frac{x}{2} + \frac{2y}{3} = -1$$

$$\Rightarrow 3x + 4y = -6 \quad \dots (i)$$

2nd equation

$$x - \frac{y}{3} = 3$$

Equation reduces to

$$3x - y = 9 \quad \dots (ii)$$

Subtracting equation (ii) from equation (i)

$$\begin{array}{r} 3x + 4y = -6 \\ 3x - y = 9 \\ \hline - \quad + \quad - \\ \hline 5y = -15 \end{array}$$

$$\Rightarrow \boxed{y = -3}$$

Putting the value of y in equation (i), we have

$$3x + 4y = -6 \quad \Rightarrow 3x + 4(-3) = -6$$

$$\Rightarrow 3x - 12 = -6$$

$$3x = 6 \quad \Rightarrow \boxed{x = 2}$$

By Substitution Method:

$$3x + 4y = -6 \quad \dots (i)$$

$$\text{and} \quad 3x - y = +9 \quad \dots (ii)$$

From equation (ii)

$$y = -9 + 3x$$

Putting this value in equation (i), we get

$$3x + 4(-9 + 3x) = -6 \quad \Rightarrow 3x - 36 + 12x = -6$$

$$\Rightarrow 3x + 12x = -6 + 36 \quad \Rightarrow 15x = 30$$

$$\Rightarrow x = \frac{30}{15} = 2 \quad \Rightarrow \boxed{x = 2}$$

Putting value of $x = 2$ in equation (ii), we have

$$3x - y = 9 \quad \Rightarrow 3(2) - y = 9$$

$$\Rightarrow 6 - y = 9 \quad \Rightarrow -y = 9 - 6$$

$$\Rightarrow -y = 3 \quad \Rightarrow \boxed{y = -3}$$



Question 2.

Form the pair of linear equations in the following problems, and find their solutions (if they exist) by the elimination method:

- (i) If we add 1 to the numerator and subtract 1 from the denominator, a fraction reduces to 1. It becomes – if we only add 1 to the denominator. What is the fraction?
- (ii) Five years ago, Nuri was thrice as old as Sonu. Ten years later, Nuri will be twice as old as Sonu. How old are Nuri and Sonu?
- (iii) The sum of the digits of a two-digit number is 9. Also, nine times this number is twice the number obtained by reversing the order of the digits. Find the number.
- (iv) Meena went to a bank to withdraw ₹ 2000. She asked the cashier to give her ₹ 50 and ₹ 100 notes only. Meena got 25 notes in all. Find how many notes of ₹ 50 and ₹ 100 she received.
- (v) A lending library has a fixed charge for the first three days and an additional charge for each day thereafter. Saritha paid ₹ 27 for a book kept for seven days, while Susy paid ₹ 21 for the book she kept for five days. Find the fixed charge and the charge for each extra day.

Solution:

(i) Let numerator be x and denominator be y .
Fraction = x/y

A.T.Q.

1st Condition:

$$\frac{x+1}{y-1} = 1 \Rightarrow x+1 = y-1$$
$$\Rightarrow x - y = -2 \quad \dots (i)$$

2nd Condition:

$$\frac{x}{y+1} = \frac{1}{2} \Rightarrow 2x = y+1$$



$$2x - y = 1 \quad \dots (ii)$$

Subtracting equation (ii) from equation (i), we get

$$\begin{array}{r} x - y = -2 \\ 2x - y = 1 \\ \hline - \quad + \quad - \\ \hline -x = -3 \end{array}$$

$$\Rightarrow \boxed{x = 3}$$

Putting $x = 3$ in equation (i),

$$\begin{aligned} 3 - y &= -2 \\ 3 + 2 &= y \Rightarrow \boxed{y = 5} \end{aligned}$$

Hence, the fraction = $\frac{x}{y} = \frac{3}{5}$

(ii) Let present age of Nuri be x years and Sonu's present age be y years.

A.T.Q.

1st Condition :

$$x - 5 = 3(y - 5) \Rightarrow x - 5 = 3y - 15$$

$$\Rightarrow x - 3y = -10 \quad \dots (i)$$

2nd Condition :

$$x + 10 = 2(y + 10) \Rightarrow x + 10 = 2y + 20$$

$$\Rightarrow x - 2y = 20 - 10 \Rightarrow x - 2y = 10 \quad \dots (ii)$$

Subtracting equation (ii) from equation (i), we get

$$\begin{array}{r} x - 3y = -10 \\ x - 2y = 10 \\ \hline - \quad + \quad - \\ \hline -y = -20 \end{array}$$

$$\Rightarrow \boxed{y = 20}$$

Putting the value of y in equation (i)

$$x - 3(20) = -10 \Rightarrow x - 60 = -10 \Rightarrow \boxed{x = 50}$$

Hence, present age of Nuri is 50 years and sonu's present age is 20 years.

(iii) Let digit at unit place = x and digit at ten's place = y .

Two digit number is $10y + x$

A.T.Q.

1st Condition :

$$x + y = 9$$

2nd Condition :

$$9(10y + x) = 2(10x + y) \Rightarrow 90y + 9x = 20x + 2y$$



$$\Rightarrow 88y - 11x = 0 \Rightarrow -11y + 88y = 0$$

$$\Rightarrow -x + 8y = 0$$

Adding equation (i) and (ii), we get

$$\begin{array}{r} x + y = 9 \\ -x + 8y = 0 \\ \hline 9y = 9 \end{array}$$

$$\Rightarrow \boxed{y = 1}$$

Putting $y = 1$ in equation (i),

$$x + 1 = 9 \Rightarrow \boxed{x = 8}$$

Number is

$$10y + x = 10(1) + 8 = 10 + 8 = 18$$

(iv) Let the number of notes of ₹ 50 = x and the number of notes of ₹ 100 = y

A.T.Q

1st Condition :

$$50x + 100y = 2000$$

$$\Rightarrow x + 2y = 40$$

2nd Condition :

$$x + y = 25$$

... (ii)

Subtracting equation (ii) from equation (i), we get

$$\begin{array}{r} x + 2y = 40 \\ x + y = 25 \\ \hline y = 15 \end{array}$$

Putting $y = 15$ in equation (i),

$$x + 2(15) = 40$$

$$x + 30 = 40$$

$$\Rightarrow \boxed{x = 10}$$

Number of notes of ₹ 50 = 10

Number of notes of ₹ 100 = 15

(v) Let, fixed charge for first 3 days be ₹ x and additional charge per day after 3 days be y .

A.T.Q.

1st Condition : as per Saritha

$$x + 4y = 27$$

2nd Condition : as per Susy



$$x + 2y = 21 \quad \dots (ii)$$

Subtracting equation (ii) from equation (i), we get

$$x + 4y = 27$$

$$x + 2y = 21$$

$$\Rightarrow \frac{2y = 6}{\quad}$$

$$\Rightarrow \boxed{y = 3}$$

Putting $y = 3$ in equation (i),

$$x + 4(3) = 27 \Rightarrow x + 12 = 27 \Rightarrow x = 15$$

Hence, fixed charge is ₹ 15 and charge for each extra day is ₹ 3.

Ex 3.5

Question 1.

Which of the following pairs of linear equations has unique solution, no solution, or infinitely many solutions. In case there is a unique solution, find it by using cross multiplication method.

(i) $x - 3y - 3 = 0$

$$3x - 9y - 2 = 0$$

(ii) $2x + y = 5$

$$3x + 2y = 8$$

(iii) $3x - 5y = 20$

$$6x - 10y = 40$$

(iv) $x - 3y - 7 = 0$

$$3x - 3y - 15 = 0$$

Solution:





(i) Equations are

$$x - 3y - 3 = 0 \text{ and } 3x - 9y - 2 = 0$$

Here,

$$\frac{a_1}{a_2} = \frac{1}{3}, \frac{b_1}{b_2} = \frac{-3}{-9} = \frac{1}{3}, \frac{c_1}{c_2} = \frac{-3}{-2} \Rightarrow \frac{a_1}{a_2} = \frac{1}{3}, \frac{b_1}{b_2} = \frac{1}{3}, \frac{c_1}{c_2} = \frac{3}{2}$$

$$\therefore \frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$$

So, pair of linear equations has no solution.

(ii) Equations are $2x + y = 5$ and $3x + 2y = 8$

$$\text{Here, } \frac{a_1}{a_2} = \frac{2}{3}, \frac{b_1}{b_2} = \frac{1}{2} \text{ and } \frac{c_1}{c_2} = \frac{5}{8}$$

$$\therefore \frac{a_1}{a_2} \neq \frac{b_1}{b_2}$$

\therefore Pair of linear equations represents unique solution.

$$\text{Now, } 2x + y = 5$$

$$\text{and } 3x + 2y = 8$$

By cross multiplication method

$$\begin{array}{ccc} & x & y & -1 \\ & 1 & 5 & 2 & 1 \\ & 2 & 8 & 3 & 2 \end{array}$$

$$\frac{x}{8-10} = \frac{y}{15-16} = \frac{-1}{4-3} \Rightarrow \frac{x}{-2} = \frac{y}{-1} = \frac{-1}{1}$$

$$\Rightarrow \boxed{x=2} \text{ and } \boxed{y=1}$$

(iii) Equations are $3x - 5y = 20$ and $6x - 10y = 40$

Here,

$$\frac{a_1}{a_2} = \frac{3}{6} = \frac{1}{2}, \frac{b_1}{b_2} = \frac{-5}{-10} = \frac{1}{2}, \frac{c_1}{c_2} = \frac{20}{40} = \frac{1}{2}$$

$$\therefore \frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$$

So, pair of linear equations has infinitely many solutions.



(iv) Equations are $x - 3y = 7$ and $3x - 3y = 15$

$$\text{Here, } \frac{a_1}{a_2} = \frac{1}{3}, \frac{b_1}{b_2} = \frac{-3}{-3}, \frac{c_1}{c_2} = \frac{7}{15} \Rightarrow \frac{a_1}{a_2} = \frac{1}{3}, \frac{b_1}{b_2} = 1, \frac{c_1}{c_2} = \frac{7}{15}$$

$$\therefore \frac{a_1}{a_2} \neq \frac{b_1}{b_2}$$

So, pair of linear equations has unique solution.

$$\text{Now } x - 3y = 7$$

$$\text{and } 3x - 3y = 15$$

By cross multiplication method

$$\begin{array}{ccc} x & y & 1 \\ -3 & -7 & 1 \\ -3 & -15 & 3 \end{array} \begin{array}{c} \nearrow \\ \searrow \\ \nearrow \\ \searrow \\ \nearrow \\ \searrow \end{array} \begin{array}{c} -3 \\ -3 \end{array}$$

$$\frac{x}{45 - 21} = \frac{y}{-21 + 15} = \frac{1}{-3 + 9} \Rightarrow \frac{x}{24} = \frac{y}{-6} = \frac{1}{6} \Rightarrow \boxed{x = 4} \text{ and } \boxed{y = -1}$$

Question 2.

(i) for which values of a and b does the following pair of linear equations have an infinite number of solutions?

$$2x + 3y = 7$$

$$(a - b)x + (a + b)y = 3a + b - 2$$

(ii) For which value of K will the following pair of linear equations have no solution?

$$3x + y = 1$$

$$(2k - 1)x + (k - 1)y = 2k + 1$$

Solution:

(i) Equations are



$$2x + 3y = 7 \quad \dots (i)$$

$$(a - b)x + (a + b)y = 3a + b - 2 \quad \dots (ii)$$

For infinitely many solutions,

$$\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2} \Rightarrow \frac{2}{a-b} = \frac{3}{a+b} = \frac{7}{3a+b-2}$$

Now, on comparing

$$\frac{2}{a-b} = \frac{3}{a+b} \Rightarrow 2(a+b) = 3(a-b) \Rightarrow 2a + 2b = 3a - 3b$$

$$\Rightarrow a - 5b = 0 \quad \dots (iii)$$

and on comparing

$$\frac{3}{a+b} = \frac{7}{3a+b-2} \Rightarrow 3(3a+b-2) = 7(a+b)$$

$$\Rightarrow 9a + 3b - 6 = 7a + 7b \Rightarrow 2a - 4b = 6$$

$\Rightarrow a - 2b = 3$ Solving (iii) and (iv) for a and b

By cross multiplication method.

$$\begin{array}{ccccc} & a & b & -1 & \\ -5 & & 0 & 1 & -5 \\ & \swarrow & \searrow & \swarrow & \searrow \\ -2 & & 3 & 1 & -2 \end{array}$$

$$\frac{a}{-15-0} = \frac{b}{0-3} = \frac{-1}{-2+5} \Rightarrow \frac{a}{-15} = \frac{b}{-3} = \frac{-1}{3} \Rightarrow \boxed{a=5} \text{ and } \boxed{b=1}$$

(ii) Equations are

$$3x + y = 1 \text{ and } (2k - 1)x + (k - 1)y = 2k + 1$$

For no solution

$$\frac{3}{2k-1} = \frac{1}{k-1} \neq \frac{1}{2k+1} \Rightarrow 3(k-1) = 2k-1$$

$$\Rightarrow 3k - 3 = 2k - 1 \Rightarrow k = 2$$

$$\text{and } \frac{1}{k-1} \neq \frac{1}{2k+1} \Rightarrow 2k + 1 \neq k - 1 \Rightarrow k \neq -2$$

$$\boxed{k=2} \text{ and } \boxed{k \neq -2}$$

Question 3.

Solve the following pair of linear equations by the substitution and cross-multiplication methods:

$$8x + 5y = 9$$

$$3x + 2y = 4$$

Solution:

Equations are



$$8x + 5y = 9 \quad \dots (i)$$

and $3x + 2y = 4 \quad \dots (ii)$

By Substitution Method:

From equation (i)

$$x = \frac{9 - 5y}{8}$$

Putting this value in equation (ii), we have

$$\Rightarrow 3 \left[\frac{9 - 5y}{8} \right] + 2y = 4 \quad \Rightarrow \frac{27 - 15y}{8} + 2y = 4$$

$$\Rightarrow 27 - 15y + 16y = 32 \quad \Rightarrow y = 5$$

Putting $y = 5$ in equation (i),

$$8x + 5(5) = 9$$

$$8x + 25 = 9$$

$$\Rightarrow 8x = -16 \quad \Rightarrow x = -2$$

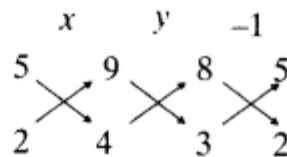
Hence, solution is $(-2, 5)$

By cross multiplication Method :

Equations are

$$8x + 5y = 9$$

and $3x + 2y = 4$



$$\frac{x}{20 - 18} = \frac{y}{27 - 32} = \frac{-1}{16 - 15} \Rightarrow \frac{x}{2} = \frac{y}{-5} = \frac{-1}{1} \Rightarrow x = -2 \text{ and } y = 5$$

Hence, solution is $(-2, 5)$

Question 4.

Form the pair of linear equations in the following problems and find their solutions (if they exist) by any algebraic method:

(i) A part of monthly hostel charges is fixed and the remaining depends on the number of days one has taken food in the mess. When a student A takes food for 20 days she has to pay ₹ 1000 as hostel charges whereas a student B, who takes food for 26 days, pays ₹ 1180 as hostel charges. Find the fixed charges and the cost of food per day.

(ii) A fraction becomes $\frac{1}{3}$ when 1 is subtracted from the numerator and it becomes $\frac{1}{4}$ when 8 is added to its denominator. Find the fraction.

(iii) Yash scored 40 marks in a test, getting 3 marks for each right answer and



losing 1 mark for each wrong answer. Had 4 marks been awarded for each correct answer and 2 marks been deducted for each incorrect answer, then Yash would have scored 50 marks. How many questions were there in the test?

(iv) Places A and B are 100 km apart on a highway. One car starts from A and another from B at the same time. If the cars travel in the same direction at different speeds, they meet in 5 hours. If they travel towards each other, they meet in 1 hour. What are the speeds of the two cars?

(v) The area of a rectangle gets reduced by 9 square units, if its length is reduced by 5 units and breadth is increased by 3 units. If we increase the length by 3 units and the breadth by 2 units, the area increases by 67 square units. Find the dimensions of the rectangle.

Solution:

(i) Let fixed monthly hostel charges = ₹ x and charges per day = ₹ y
A.T.Q.

As per condition of student A

$$x + 20y = 1000$$

As per condition of student B

$$x + 26y = 1180$$

By cross multiplication method

$$\begin{array}{ccc} x & y & -1 \\ 20 & 1000 & 1 \\ 26 & 1180 & 1 \end{array}$$

$$\frac{x}{23600 - 26000} = \frac{y}{1000 - 1180} = \frac{-1}{26 - 20}$$

$$\Rightarrow \frac{x}{-2400} = \frac{y}{-180} = \frac{-1}{6} \Rightarrow x = \frac{2400}{6} = 400 \Rightarrow x = 400$$

$$\text{and } y = \frac{180}{6} = 30 \Rightarrow y = 30$$

∴ Fixed monthly hostel charges = ₹ 400 and charges per day = ₹ 30



(ii) Let numerator = x and denominator = y

\therefore Fraction = $\frac{x}{y}$

A.T.Q.

1st Condition:

$$\frac{x-1}{y} = \frac{1}{3} \Rightarrow 3x - 3 = y \Rightarrow 3x - y = 3 \quad \dots (i)$$

2nd Condition:

$$\frac{x}{y+8} = \frac{1}{4} \Rightarrow 4x = y + 8 \quad \dots (ii)$$

$$\Rightarrow 4x - y = 8$$

Solving (i) and (ii) for x and y

By cross multiplication method

$$\begin{array}{ccccccc} & x & & y & & -1 & \\ & -1 & \times & 3 & \times & 3 & \times & -1 \\ & -1 & \times & 8 & \times & 4 & \times & -1 \\ \Rightarrow & \frac{x}{-8+3} & = & \frac{y}{12-24} & = & \frac{-1}{-3+4} & \Rightarrow & \frac{x}{-5} = \frac{y}{-12} = \frac{-1}{1} \Rightarrow \boxed{x=5} \text{ and } \boxed{y=12} \end{array}$$

\therefore Fraction = $\frac{5}{12}$

(iii) Let number of right answers = x

Number of wrong answers = y

Total questions are $x + y$

A.T.Q.

1st Condition:

$$3x - y = 40 \quad \dots (i)$$

2nd Condition:

$$4x - 2y = 50 \quad \dots (ii)$$

Solving (i) and (ii) for x and y





By cross multiplication method

$$\begin{array}{ccc} & x & y & -1 \\ -1 & \searrow & \nearrow & 3 & \searrow & -1 \\ & 40 & & 4 & & -2 \\ -2 & \nearrow & \searrow & 50 & & \end{array}$$
$$\frac{x}{-50 + 80} = \frac{y}{160 - 150} = \frac{-1}{-6 + 4} \Rightarrow \frac{x}{30} = \frac{y}{10} = \frac{-1}{-2}$$
$$\Rightarrow \boxed{x = 15} \text{ and } \boxed{y = 5}$$

\therefore Total questions are $15 + 5 = 20$.

(iv) Let speed of car starting from point A = x km/h

Speed of car starting from point B = y km/h

A.T.Q.

1st Condition:

If the cars travel in same direction, then

$$5x - 5y = 100$$

or, $x - y = 20$... (i)

If they travel in opposite directions, then

$$x + y = 100 \quad \dots (ii)$$

Solving (i) and (ii) for x and y





By cross multiplication method

$$\begin{array}{ccc} & x & y & -1 \\ -1 & \swarrow & \searrow & \swarrow & \searrow & \swarrow & \searrow \\ & 20 & 1 & -1 \\ 1 & \swarrow & \searrow & \swarrow & \searrow & \swarrow & \searrow \\ & 100 & 1 & 1 \end{array}$$
$$\Rightarrow \frac{x}{-100 - 20} = \frac{y}{20 - 100} = \frac{-1}{1 + 1} \Rightarrow \frac{x}{-120} = \frac{y}{-80} = \frac{-1}{2}$$

$$\Rightarrow x = \frac{120}{2} = 60 \text{ and } y = \frac{80}{2} = 40$$

$$\therefore \boxed{x = 60 \text{ km/h}} \text{ and } \boxed{y = 40 \text{ km/h}}$$

\therefore Speed of car starting from point A = 60 km/h

Speed of car starting from point B = 40 km/h.

(v) Let length and breadth of the rectangle be x and y respectively.

$$\therefore \text{Area} = xy$$

A.T.Q.

1st Condition:

$$(x - 5)(y + 3) = xy - 9 \Rightarrow xy + 3x - 5y - 15 = xy - 9$$

$$\Rightarrow 3x - 5y - 15 = -9$$

$$\Rightarrow 3x - 5y = 6 \quad \dots (i)$$





2nd Condition:

$$(x + 3)(y + 2) = xy + 67 \Rightarrow xy + 2x + 3y + 6 = xy + 67$$
$$\Rightarrow 2x + 3y + 6 = 67$$
$$\Rightarrow 2x + 3y = 61 \quad \dots (ii)$$

Solving equations (i) and (ii)

By cross multiplication method

$$\begin{array}{ccc} & x & y & -1 \\ -5 & \nearrow 6 & \nearrow 3 & \nearrow -5 \\ & 3 & 61 & 2 & 3 \end{array}$$
$$\frac{x}{-305 - 18} = \frac{y}{12 - 183} = \frac{-1}{9 + 10} \Rightarrow \frac{x}{-323} = \frac{y}{-171} = \frac{-1}{19}$$
$$\Rightarrow x = \frac{323}{19} = 17 \Rightarrow \boxed{x = 17 \text{ units}}$$

and $y = \frac{171}{19} = 9 \Rightarrow \boxed{y = 9 \text{ units}}$

\therefore Length of rectangle = 17 units
and breadth of rectangle = 9 units

NCERT Solutions For Class 10 Maths Chapter 3 Exercise 3.6 Question 1.

Solve the following pairs of equations by reducing them to a pair of linear equations:



$$(i) \quad \frac{1}{2x} + \frac{1}{3y} = 2$$

$$\frac{1}{3x} + \frac{1}{2y} = \frac{13}{6}$$

$$(iii) \quad \frac{4}{x} + 3y = 14$$

$$\frac{3}{x} - 4y = 23$$

$$(v) \quad \frac{7x - 2y}{xy} = 5$$

$$\frac{8x + 7y}{xy} = 15$$

$$(vii) \quad \frac{10}{x+y} + \frac{2}{x-y} = 4,$$

$$\frac{15}{x+y} - \frac{5}{x-y} = -2$$

$$(ii) \quad \frac{2}{\sqrt{x}} + \frac{3}{\sqrt{y}} = 2$$

$$\frac{4}{\sqrt{x}} - \frac{9}{\sqrt{y}} = -1$$

$$(iv) \quad \frac{5}{x-1} + \frac{1}{y-2} = 2$$

$$\frac{6}{x-1} - \frac{3}{y-2} = 1$$

$$(vi) \quad 6x + 3y = 6xy$$

$$2x + 4y = 5xy$$

$$(viii) \quad \frac{1}{3x+y} + \frac{1}{3x-y} = \frac{3}{4}$$

$$\frac{1}{2(3x+y)} - \frac{1}{2(3x-y)} = \frac{-1}{8}$$

Solution:

$$(i) \quad \frac{1}{2x} + \frac{1}{3y} = 2 \quad \dots (i)$$

$$\frac{1}{3x} + \frac{1}{2y} = \frac{13}{6} \quad \dots (ii)$$

Putting $\frac{1}{x} = u$ and $\frac{1}{y} = v$ in eq. (i) and eq. (ii), we get

$$\frac{1}{2}u + \frac{1}{3}v = 2 \Rightarrow \frac{3u + 2v}{6} = 2$$

$$\Rightarrow 3u + 2v = 12 \quad \dots (iii)$$

From eq. (ii)

$$\frac{1}{3}u + \frac{1}{2}v = \frac{13}{6} \Rightarrow \frac{2u + 3v}{6} = \frac{13}{6}$$

$$\Rightarrow 2u + 3v = 13 \quad \dots (iv)$$

Solving (iii) and (iv) for u and v

By cross multiplication method



$$\begin{array}{ccc}
 & u & v & -1 \\
 2 & \searrow & 12 & \searrow & 3 & \searrow & 2 \\
 & 3 & \swarrow & 13 & \swarrow & 2 & \swarrow & 3 \\
 \Rightarrow & \frac{u}{26-36} & = & \frac{v}{24-39} & = & \frac{-1}{9-4} \\
 & \frac{u}{-10} & = & \frac{v}{-15} & = & \frac{-1}{5} \\
 & u = 2, v = 3
 \end{array}$$

$$\therefore x = \frac{1}{u} = \frac{1}{2} \text{ and } y = \frac{1}{v} = \frac{1}{3}$$

$$(ii) \quad \frac{2}{\sqrt{x}} + \frac{3}{\sqrt{y}} = 2 \quad \dots (i)$$

$$\text{and} \quad \frac{4}{\sqrt{x}} - \frac{9}{\sqrt{y}} = -1 \quad \dots (ii)$$

Put $\frac{1}{\sqrt{x}} = u$ and $\frac{1}{\sqrt{y}} = v$ in eq. (i) and (ii).

$$\text{From eq. (i)} \quad 2u + 3v = 2 \quad \dots (iii)$$

$$\text{From eq. (ii)} \quad 4u - 9v = -1 \quad \dots (iv)$$

Solving for u and v .

By cross multiplication method

$$\begin{array}{ccc}
 & u & v & -1 \\
 3 & \searrow & 2 & \searrow & 2 & \searrow & 3 \\
 & -9 & \swarrow & -1 & \swarrow & 4 & \swarrow & -9
 \end{array}$$

$$\frac{u}{-3+18} = \frac{v}{8+2} = \frac{-1}{-18-12} \Rightarrow \frac{u}{15} = \frac{v}{10} = \frac{1}{30} \Rightarrow u = \frac{1}{2} \text{ and } v = \frac{1}{3}$$

$$\text{but } u = \frac{1}{\sqrt{x}} = \frac{1}{2} \text{ and } v = \frac{1}{\sqrt{y}} = \frac{1}{3} \Rightarrow \boxed{x=4} \text{ and } \boxed{y=9}$$

$$(iii) \quad \frac{4}{x} + 3y = 14 \quad \dots (i)$$

$$\text{and} \quad \frac{3}{x} - 4y = 23 \quad \dots (ii)$$

Put $\frac{1}{x} = u$ in eq. (i) and eq. (ii), we get

$$4u + 3y = 14 \quad \dots (iii)$$

$$\text{and} \quad 3u - 4y = 23 \quad \dots (iv)$$

Solving (iii) and (iv) for u and y



By cross multiplication method

$$\begin{array}{ccc}
 u & y & -1 \\
 3 & 14 & 4 & 3 \\
 -4 & \times & 23 & \times & 3 & \times & -4
 \end{array}$$

$$\frac{u}{69+56} = \frac{y}{42-92} = \frac{-1}{-16-9} \Rightarrow \frac{u}{125} = \frac{y}{-50} = \frac{-1}{-25} \Rightarrow u = \frac{125}{25} = 5,$$

$$y = \frac{-50}{25} = -2$$

$$\therefore \frac{1}{x} = 5 \Rightarrow \boxed{x = \frac{1}{5}} \text{ and } \boxed{y = -2}$$

$$(iv) \quad \frac{5}{x-1} + \frac{1}{y-2} = 2 \quad \dots (i)$$

$$\text{and } \frac{6}{x-1} - \frac{3}{y-2} = 1 \quad \dots (ii)$$

Put $\frac{1}{x-1} = u$ and $\frac{1}{y-2} = v$ in eq. (i) and eq. (ii),
we get

$$5u + v = 2 \quad \dots (iii)$$

$$\text{and } 6u - 3v = 1 \quad \dots (iv)$$

Solving equation (iii) and (iv)

By cross multiplication method

$$\begin{array}{ccc}
 u & v & -1 \\
 1 & 2 & 5 & 1 \\
 -3 & \times & 1 & \times & 6 & \times & -3
 \end{array}$$

$$\frac{u}{1+6} = \frac{v}{12-5} = \frac{-1}{-15-6} \Rightarrow \frac{u}{7} = \frac{v}{7} = \frac{-1}{-21} \Rightarrow u = \frac{1}{3} \text{ and } v = \frac{1}{3}$$

$$\therefore x-1 = \frac{1}{u} = 3 \text{ and } y-2 = \frac{1}{v} = 3 \Rightarrow \boxed{x=4} \text{ and } \boxed{y=5}$$

$$(v) \quad \frac{7x-2y}{xy} = 5 \text{ and } \frac{8x+7y}{xy} = 15$$

$$\Rightarrow \frac{7}{y} - \frac{2}{x} = 5 \quad \dots (i)$$

$$\text{and } \frac{8}{y} + \frac{7}{x} = 15 \quad \dots (ii)$$

Putting $\frac{1}{y} = u$ and $\frac{1}{x} = v$ in eq. (i) and eq. (ii), we get

$$7u - 2v = 5 \text{ and } 8u + 7v = 15$$

solving for u and v by cross multiplication method:



$$\begin{array}{ccccc}
 & u & v & -1 & \\
 -2 & & 5 & & 7 & -2 \\
 & \swarrow & \searrow & \swarrow & \searrow & \\
 7 & & 15 & & 8 & & 7
 \end{array}$$

$$\frac{u}{-30-35} = \frac{v}{40-105} = \frac{-1}{49+16} \Rightarrow \frac{u}{-65} = \frac{v}{-65} = \frac{-1}{65} \Rightarrow u = \frac{65}{65}, v = \frac{65}{65}$$

$$\Rightarrow \boxed{y=1} \text{ and } \boxed{x=1}$$

$$(vi) \quad 6x + 3y = 6xy$$

$$\Rightarrow \frac{6}{y} + \frac{3}{x} = 6 \quad \text{(dividing by } xy \text{ both sides) ... (i)}$$

$$\text{Also, } 2x + 4y = 5xy$$

$$\Rightarrow \frac{2}{y} + \frac{4}{x} = 5 \quad \text{... (ii)}$$

Putting $\frac{1}{y} = u$ and $\frac{1}{x} = v$ in eqs. (i) and (ii), we get

$$6u + 3v = 6 \quad \text{... (iii)}$$

$$\text{and } 2u + 4v = 5 \quad \text{... (iv)}$$

Solving (iii) and (iv) for u and v

By cross multiplication method:

$$\begin{array}{ccccc}
 & u & v & -1 & \\
 3 & & 6 & & 6 & 3 \\
 & \swarrow & \searrow & \swarrow & \searrow & \\
 4 & & 5 & & 2 & & 4
 \end{array}$$

$$\frac{u}{15-24} = \frac{v}{12-30} = \frac{-1}{24-6} \Rightarrow \frac{u}{-9} = \frac{v}{-18} = \frac{-1}{18} \Rightarrow u = \frac{1}{2} \text{ and } v = 1$$

$$\Rightarrow \boxed{y=2} \text{ and } \boxed{x=1}$$

$$(vii) \quad \frac{10}{x+y} + \frac{2}{x-y} = 4 \quad \text{... (i)}$$

$$\text{and } \frac{15}{x+y} - \frac{5}{x-y} = -2 \quad \text{... (ii)}$$

Put $\frac{1}{x+y} = X$ and $\frac{1}{x-y} = Y$ in eq. (i) and eq. (ii), we get

$$10X + 2Y = 4 \quad \text{... (iii)}$$

$$\text{and } 15X - 5Y = -2 \quad \text{... (iv)}$$

On solving (iii) and (iv) for X and Y

By cross multiplication method:



$$\begin{array}{ccccccc}
 & & X & & Y & & -1 \\
 & & 2 & & 4 & & 10 & & 2 \\
 & & \swarrow & \searrow & \swarrow & \searrow & \swarrow & \searrow & \\
 & & -5 & & -2 & & 15 & & -5 \\
 \\
 & \frac{X}{-4+20} & = & \frac{Y}{60+20} & = & \frac{-1}{-50-30} & \Rightarrow & \frac{X}{16} & = & \frac{Y}{80} & = & \frac{-1}{-80}
 \end{array}$$

Hence $X = \frac{1}{5}$ and $Y = 1 \Rightarrow \frac{1}{x+y} = \frac{1}{5}$ and $\frac{1}{x-y} = 1$

$\Rightarrow x + y = 5$... (v)

and $x - y = 1$... (vi)

On solving (v) and (vi) for x and y , we get

$\Rightarrow \boxed{x=3}$ and $\boxed{y=2}$

(viii) $\frac{1}{3x+y} + \frac{1}{3x-y} = \frac{3}{4}$... (i)

$\frac{1}{2(3x+y)} - \frac{1}{2(3x-y)} = \frac{-1}{8}$... (ii)

Put $\frac{1}{3x+y} = X$ and $\frac{1}{3x-y} = Y$ in eq. (i) and eq. (ii), we get

$$X + Y = \frac{3}{4}$$

$\Rightarrow 4X + 4Y = 3$... (iii)

$$\frac{1(X)}{2} - \frac{1(Y)}{2} = \frac{-1}{8}$$

$$\frac{X}{2} - \frac{Y}{2} = \frac{-1}{8}$$

$4X - 4Y = -1$... (iv)

Solving (iii) and (iv) for X and Y .

On adding (iii) and (iv), we have

$$8X = 2 \Rightarrow X = \frac{2}{8} = \frac{1}{4}$$

On subtracting (iv) from (iii), we have

$$8Y = 4 \Rightarrow Y = \frac{1}{2}$$

$\therefore \frac{1}{3x+y} = \frac{1}{4}$ and $\frac{1}{3x-y} = \frac{1}{2}$



$$\begin{aligned} & 3x + y = 4 && \dots (v) \\ \text{and} & 3x - y = 2 && \dots (vi) \\ \text{On adding (v) and (vi), we get} & 6x = 6 \Rightarrow && \boxed{x = 1} \\ \text{On subtracting (vi) from (v)} & && \\ & 2y = 2 \Rightarrow && \boxed{y = 1} \end{aligned}$$

NCERT Solutions For Class 10th Maths Chapter 3 Exercise 3.6 Question 2.

Formulate the following problems as a pair of equations, and hence find their solutions:

- (i) Ritu can row downstream 20 km in 2 hours, and upstream 4 km in 2 hours. Find her speed of rowing in still water and the speed of the current.
- (ii) 2 women and 5 men can together finish an embroidery work in 4 days, while 3 women and 6 men can finish it in 3 days. Find the time taken by 1 woman alone to finish the work, and also that taken by 1 man alone.
- (iii) Roohi travels 300 km to her home partly by train and partly by bus. She takes 4 hours if she travels 60 km by train and the remaining by bus. If she travels 100 km by train and the remaining by bus, she takes 10 minutes longer. Find the speed of the train and the bus separately.

Solution:

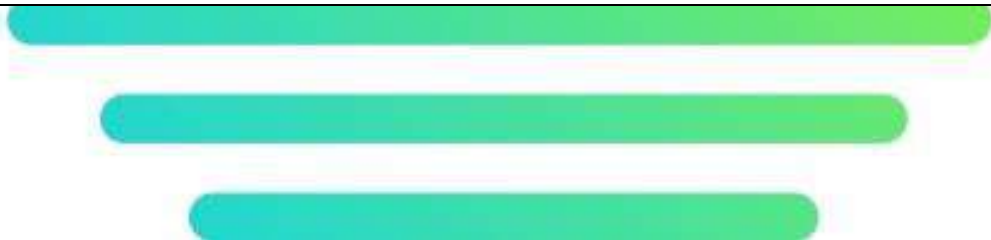
- (i) Let Ritu's speed in still water = x km/h
Speed of current = y km/h
During downstream, speed = $(x + y)$ km/h
During upstream, speed = $(x - y)$ km/h

A.T.Q.

1st condition :

$$x + y = 20/2 \Rightarrow x + y = 10$$

2nd condition :





$$x - y = \frac{4}{2} \quad \Rightarrow x - y = 2 \quad \dots(ii)$$

Adding (i) and (ii)

$$2x = 12 \quad \Rightarrow x = 6$$

Putting $x = 6$ in eq. (i)

$$6 + y = 10 \quad \Rightarrow y = 4 \quad \Rightarrow \boxed{x = 6 \text{ km/h}} \text{ and } \boxed{y = 4 \text{ km/h}}$$

\therefore Ritu's speed in still water = 6 km/h

Speed of current = 4 km/h

- (ii) Let time taken by 1 woman to finish the work = x days and time taken by 1 man to finish the work = y days.

A.T.Q.

1st Condition:

$$\frac{2}{x} + \frac{5}{y} = \frac{1}{4} \quad \dots (i)$$

2nd Condition:

$$\frac{3}{x} + \frac{6}{y} = \frac{1}{3} \quad \dots (ii)$$

Operating (i) $\times 3$ - (ii) $\times 2$

$$\frac{6}{x} + \frac{15}{y} = \frac{3}{4}$$

$$\frac{6}{x} + \frac{12}{y} = \frac{2}{3}$$

$$\begin{array}{r} \frac{6}{x} + \frac{15}{y} = \frac{3}{4} \\ \frac{6}{x} + \frac{12}{y} = \frac{2}{3} \\ \hline \frac{3}{y} = \frac{3}{4} - \frac{2}{3} \end{array}$$

$$\therefore \frac{3}{y} = \frac{9-8}{12} \quad \therefore \frac{3}{y} = \frac{1}{12} \Rightarrow \boxed{y = 36 \text{ days}}$$

Putting $y = 36$ in eq. (i)

$$\frac{2}{x} + \frac{5}{36} = \frac{1}{4} \Rightarrow \frac{2}{x} = \frac{1}{4} - \frac{5}{36} \Rightarrow \frac{2}{x} = \frac{9-5}{36} \Rightarrow \frac{2}{x} = \frac{4}{36} \Rightarrow \boxed{x = 18 \text{ days}}$$

Time taken by 1 woman to finish the work = 18 days.

Time taken by 1 man to finish the work = 36 days.

- (iii) Let speed of train = x km/h and Speed of bus = y km/h

Total distance = 300 km

A.T.Q.

1st condition :



$$\frac{60}{x} + \frac{240}{y} = 4 \quad \dots (i)$$

2nd condition :

$$\frac{100}{x} + \frac{200}{y} = 4 + \frac{10}{60} \Rightarrow \frac{100}{x} + \frac{200}{y} = \frac{25}{6} \quad \dots (ii)$$

Operating eq. (i) $\times 100$ - eq. (ii) $\times 60$

$$\begin{array}{r} \frac{6000}{x} + \frac{24000}{y} = 400 \\ \frac{6000}{x} + \frac{12000}{y} = 250 \\ \hline \frac{12000}{y} = 150 \end{array}$$

$$\Rightarrow y = \frac{12000}{150} \Rightarrow y = 80 \Rightarrow \boxed{y = 80 \text{ km/h}}$$

Putting $y = 80$ in equation (i)

$$\frac{60}{x} + \frac{240}{80} = 4 \Rightarrow \frac{60}{x} + 3 = 4 \Rightarrow \frac{60}{x} = 1 \Rightarrow x = 60 \text{ km/h}$$

\therefore Speed of the train = 60 km/h

Speed of the bus = 80 km/h

Ex 3.7

Question 1.

The age of two friends Ani and Biju differ by 3 years. Ani's father Dharam is twice as old as Ani and Biju is twice as old as his sister Cathy. The ages of Cathy and Dharam differ by 30 years. Find the ages of Ani and Biju.

Solution:

Let the ages of Ani and Biju be x years and y years respectively.

If Ani is older than Biju

$$x - y = 3$$

If Biju is older than Ani

$$y - x = 3$$

$$-x + y = 3 \quad [\text{Given}]$$



Dharm's age = $2x$ years and Cathy's age = $\frac{y}{2}$ years

Clearly, Dharam is older than Cathy.

$$\therefore 2x - \frac{y}{2} = 30$$

$$\Rightarrow 4x - y = 60$$

Thus, we have the following two systems of linear equations:

$$x - y = 3 \quad \dots(\text{i})$$

$$4x - y = 60 \quad \dots(\text{ii})$$

And $x - y = -3 \quad \dots(\text{iii})$

$$4x - y = 60 \quad \dots(\text{iv})$$

Subtracting equation (i) from equation (ii), we get:

$$3x - 57$$

$$\Rightarrow x = 19$$

Putting $x = 19$ in equation (i), we get

$$19 - y = 3$$

$$\Rightarrow y = 16$$

Again subtracting equation (iv) from equation (iii), we get

$$3x = 63$$

$$\Rightarrow x = 21$$

Putting $x = 21$ in equation (iii) we get

$$21 - y = -3$$

$$\Rightarrow y = 24$$

Hence, Ani's age is either 19 years or 21 years and Biju's age is either 16 years or 24 years.

Question 2.

One says, "Give me a hundred, friend! I shall then become twice as rich as you". The other replies, "If you give me ten, I shall be six times as rich as you". Tell me what is the amount of their (respective) capital?

Solution:

Let the two friends have ₹ x and ₹ y .

According to the first condition:

One friend has an amount = ₹ $(x + 100)$

Other has an amount = ₹ $(y - 100)$

$$\therefore (x + 100) = 2(y - 100)$$



$$\Rightarrow x + 100 = 2y - 200$$

$$\Rightarrow x - 2y = -300 \quad \dots(i)$$

According to the second condition:

One friend has an amount = ₹(x - 10)

Other friend has an amount = ₹(y + 10)

$$\therefore 6(x - 10) = y + 10$$

$$\Rightarrow 6x - 60 = y + 10$$

$$\Rightarrow 6x - y = 70 \quad \dots(ii)$$

Multiplying (ii) equation by 2 and subtracting the result from equation (i), we get:

$$x - 12x = -300 - 140$$

$$\Rightarrow -11x = -440$$

$$\Rightarrow x = 40$$

Substituting x = 40 in equation (ii), we get

$$6 \times 40 - y = 70$$

$$\Rightarrow -y = 70 - 24$$

$$\Rightarrow y = 170$$

Thus, the two friends have ₹ 40 and ₹ 170.

Question 3.

A train covered a certain distance at a uniform speed. If the train would have been 10 km/h faster, it would have taken 2 hours less than the scheduled time. And, if the train were slower by 10 km/h, it would have taken 3 hours more than the scheduled time. Find the distance covered by the train.

Solution:

Let the original speed of the train be x km/h

and the time taken to complete the journey be y hours.

Then the distance covered = xy km

Case I: When speed = (x + 10) km/h and time taken = (y - 2) h

Distance = (x + 10) (y - 2) km

$$\Rightarrow xy = (x + 10) (y - 2)$$

$$\Rightarrow 10y - 2x = 20$$

$$\Rightarrow 5y - x = 10$$

$$\Rightarrow -x + 5y = 10 \quad \dots(i)$$

Case II: When speed = (x - 10) km/h and time taken = (y + 3) h

Distance = (x - 10) (y + 3) km

$$\Rightarrow xy = (x - 10) (y + 3)$$

$$\Rightarrow 3x - 10y = 30 \quad \dots(ii)$$

Multiplying equation (i) by 3 and adding the result to equation (ii), we get

$$15y - 10y = 30 + 30$$

$$\Rightarrow 5y = 60$$



$$\Rightarrow y = 12$$

Putting $y = 12$ in equation (ii), we get

$$3x - 10 \times 12 = 30$$

$$\Rightarrow 3x = 150$$

$$\Rightarrow x = 50$$

$$\therefore x = 50 \text{ and } y = 12$$

Thus, original speed of train is 50 km/h and time taken by it is 12 h.

Distance covered by train = Speed \times Time

$$= 50 \times 12 = 600 \text{ km.}$$

Question 4.

The students of a class are made to stand in rows. If 3 students are extra in a row, there would be 1 row less. If 3 students are less in a row, there would be 2 rows more. Find the number of students in the class.

Solution:

Let the number of rows be x and the number of students in each row be y .

Then the total number of students = xy

Case I: When there are 3 more students in each row

Then the number of students in a row = $(y + 3)$

and the number of rows = $(x - 1)$

Total number of students = $(x - 1)(y + 3)$

$$\therefore (x - 1)(y + 3) = xy$$

$$\Rightarrow 3x - y = 3 \dots(i)$$

Case II: When 3 students are removed from each row

Then the number of students in each row = $(y - 3)$

and the number of rows = $(x + 2)$

Total number of students = $(x + 2)(y - 3)$

$$\therefore (x + 2)(y - 3) = xy$$

$$\Rightarrow -3x + 2y = 6 \dots(ii)$$

Adding the equations (i) and (ii), we get

$$-y + 2y = 3 + 6$$

$$\Rightarrow y = 9$$

Putting $y = 9$ in the equation (ii), we get

$$-3x + 18 = 6$$

$$\Rightarrow x = 4$$

$$\therefore x = 4 \text{ and } y = 9$$

Hence, the total number of students in the class is $9 \times 4 = 36$.

Question 5.

In a $\triangle ABC$, $\angle C = 3 \angle B = 2(\angle A + \angle B)$. Find the three angles.

Solution:

Let $\angle A = x^\circ$ and $\angle B = y^\circ$.



Then $\angle C = 3\angle B = (3y)^\circ$.

Now $\angle A + \angle B + \angle C = 180^\circ$

$$\Rightarrow x + y + 3y = 180^\circ$$

$$\Rightarrow x + 4y = 180^\circ \dots(i)$$

Also, $\angle C = 2(\angle A + \angle B)$

$$\Rightarrow 3y - 2(x + y)$$

$$\Rightarrow 2x - y = 0^\circ \dots(ii)$$

Multiplying (ii) by 4 and adding the result to equation (i), we get:

$$9x = 180^\circ$$

$$\Rightarrow x = 20^\circ$$

Putting $x = 20$ in equation (i), we get:

$$20 + 4y = 180^\circ$$

$$\Rightarrow 4y = 160^\circ$$

$$\Rightarrow y = \frac{160}{4} = 40^\circ$$

$$\therefore \angle A = 20^\circ, \angle B = 40^\circ \text{ and } \angle C = 3 \times 40^\circ = 120^\circ.$$

Question 6.

Draw the graphs of the equations $5x - y = 5$ and $3x - y = 3$. Determine the coordinates of the vertices of the triangle formed by these lines and the y-axis.

Solution:

$$5x - y = 5 \dots(i)$$

$$3x - y = 3 \dots(ii)$$

For graphical representation:

From equation (i), we get: $y = 5x - 5$

When $x = 0$, then $y = -5$

When $x = 2$, then $y = 10 - 5 = 5$

When $x = 1$, then $y = 5 - 5 = 0$

Thus, we have the following table of solutions:

x	0	2	1
y	-5	5	0

From equation (ii), we get:

$$\Rightarrow y = 3x - 3$$

When $x = 0$, then $y = -3$

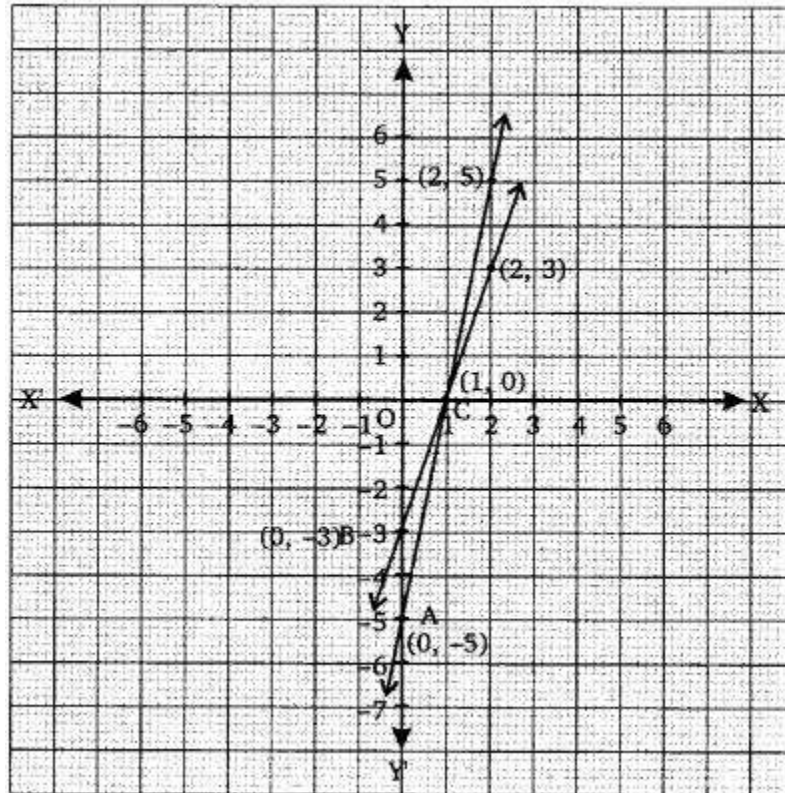
When $x = 2$, then $y = 6 - 3 = 3$

When $x = 1$, then $y = 3 - 3 = 0$

Thus, we have the following table of solutions:

x	0	2	1
y	-3	3	0

Plotting the points of each table of solutions, we obtain the graphs of two lines intersecting each other at a point $C(1, 0)$.



The vertices of $\triangle ABC$ formed by these lines and the y-axis are $A(0, -5)$, $B(0, -3)$ and $C(1, 0)$.

Question 7.

Solve the following pairs of linear equations:

(i) $px + qy = p - q$

$$qx - py = p + q$$

(ii) $ax + by = c$

$$bx + ay = 1 + c$$

(iii) $\frac{x}{a} - \frac{y}{b} = 0$

$$ax + by = a^2 + b^2$$

(iv) $(a - b)x + (a + b)y = a^2 - 2ab - b^2$

$$(a + b)(x + y) = a^2 + b^2$$

(v) $152x - 378y = -74$

$$-378x + 152y = -604$$



Solution:

(i) The given equations are

$$px + qy = p - q \dots(1)$$

$$qx - py = p + q \dots(2)$$

Multiplying equation (1) by q and equation (2) by p and then adding the results, we get:

$$x(p^2 + q^2) = p(p - q) + q(p + q)$$

$$\Rightarrow x = \frac{p(p - q)}{p^2 + q^2} + \frac{q(p + q)}{p^2 + q^2}$$

$$\Rightarrow x = \frac{p^2 - pq + qp + q^2}{p^2 + q^2}$$

$$\Rightarrow x = \frac{p^2 + q^2}{p^2 + q^2} = 1.$$

Putting $x = 1$ in equation (ii), we get:

$$q \times 1 - py = p + q$$

$$\Rightarrow q \times 1 - py = p + q$$

$$\Rightarrow y = \frac{-p}{p} = -1.$$

Thus, $x = 1$ and $y = -1$ is the required solution.

(ii) The given equations are

$$ax + by = c \dots(1)$$

$$bx - ay = 1 + c \dots(2)$$

Multiplying equation (1) by b and equation (2) by a , we get:

$$abx + b^2y = cb \dots(3)$$

$$abx + a^2y = a(1 + c) \dots(4)$$

Subtracting (3) from (4), we get:



$$(b^2 - a^2)y = cb - a - ac$$

$$\Rightarrow y = \frac{c(b - a) - a}{b^2 - a^2}$$

$$\Rightarrow y = \frac{c(a - b) + a}{a^2 - b^2}$$

Putting $y = \frac{c(a - b) + a}{a^2 - b^2}$ in equation (2), we get

$$bx + a \left[\frac{c(a - b) + a}{a^2 - b^2} \right] = 1 + c$$

$$\Rightarrow bx = 1 + c - a \left[\frac{c(a - b) + a}{a^2 - b^2} \right]$$

$$\Rightarrow bx = 1 + c - a \left[\frac{ca - cb + a}{a^2 - b^2} \right]$$
$$= \frac{a^2 - b^2 + a^2c - b^2c - a^2c + abc - a^2}{a^2 - b^2}$$

$$= \frac{-b^2 - b^2c + abc}{a^2 - b^2}$$

$$= \frac{b(-b - cb + ac)}{a^2 - b^2}$$

$$\Rightarrow x = \frac{-b - cb + ac}{a^2 - b^2}$$

$$= \frac{c(a - b) - b}{a^2 - b^2} = \frac{c(a - b) - b}{a^2 - b^2}$$

Thus, $x = \frac{c(a - b) - b}{a^2 - b^2}$ and $y =$

$\frac{c(a - b) - b}{a^2 - b^2}$ is the required solution.



(iii) The given equations may be written as: $bx - ay = 0$...(1)

$ax + by = a^2 + b^2$...(2)

Multiplying equation (1) by b and equation (2) by a , we get:

$b^2x + aby = 0$ (3)

$a^2x + aby = a(a^2 + b^2)$ (4)

Adding equation (3) and equation (4), we get:

$(a^2 + b^2)x = a(a^2 + b^2)$

$$(a^2 + b^2)x = a(a^2 + b^2)$$

$$\Rightarrow x = \frac{a(a^2 + b^2)}{a^2 + b^2} = a$$

Putting $x = a$ in equation (2), we get:

$$a \times a + by = a^2 + b^2$$

$$\Rightarrow a \times a + by = a^2 + b^2$$

$$\Rightarrow y = \frac{a^2 + b^2 - a^2}{b} = b$$

$$\Rightarrow y = b$$

Thus, $x = a$ and $y = b$ is the required solution.

(iv) The given equations may be written as:

$(a - b)x + (a + b)y = a^2 - 2ab - b^2$...(1)

$(a + b)x + (a + b)y = a^2 + b^2$...(2)

Subtracting equation (2) from equation (1), we get:

$(a - b)x - (a + b)x$

$= (a^2 - 2ab - b^2) - (a^2 + b^2)$

$\Rightarrow x(a - b - a - b) = a^2 - 2ab - b^2 - a^2 - b^2$

$\Rightarrow -2bx = -2ab - 2b^2$

$\Rightarrow 2bx = 2b^2 + 2ab$



$$\Rightarrow x = \frac{b(a+b)}{b} = a + b$$

$$\Rightarrow x = a + b$$

Substituting $x = a + b$ in equation (1), we get:

$$(a - b)(a + b) + (a + b)y = a^2 - 2ab - b^2$$

$$\Rightarrow a^2 - b^2 + (a + b)y = a^2 - 2ab - b^2$$

$$\Rightarrow (a + b)y = a^2 - 2ab - b^2 - a^2 + b^2$$

$$\Rightarrow y = \frac{-2ab}{a + b}$$

Thus, $x = a + b$ and $y = \frac{-2ab}{a + b}$ is the required solution.

(v) The given equations may be written as:

$$76x - 189y = -37 \dots(1)$$

$$-189x + 76y = -302 \dots(2)$$

Multiplying equation (1) by 76 and equation (2) by 189, we get:

$$5776x - 14364y = -2812 \dots(3)$$

$$-35721x + 14364y = -57078 \dots(4)$$

Adding equations (3) and (4), we get:

$$5776x - 35721x = -2812 - 57078$$

$$\Rightarrow -29945x = -59890$$

$$\Rightarrow x = 2$$

Putting $x = 2$ in equation (1), we get:

$$76 \times 2 - 189y = -37$$

$$\Rightarrow 152 - 189y = -37$$

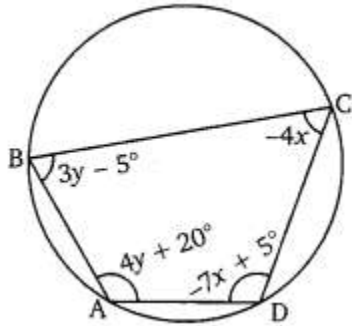
$$\Rightarrow -189y = -189$$

$$\Rightarrow y = 1$$

Thus, $x = 2$ and $y = 1$ is the required solution.

Question 8.

ABCD is a cyclic quadrilateral (see figure). Find the angles of the cyclic quadrilateral.



Solution:





We know that the sum of opposite angles of a cyclic quadrilateral is 180° .

$$\begin{aligned}\therefore \quad \angle B + \angle D &= 180^\circ \\ \Rightarrow 3y - 5^\circ + (-7x + 5^\circ) &= 180^\circ \\ \Rightarrow 3y - 5^\circ - 7x + 5^\circ &= 180^\circ \\ \Rightarrow -7x + 3y &= 180^\circ \\ \Rightarrow 7x - 3y &= -180^\circ \quad \dots(i)\end{aligned}$$

$$\begin{aligned}\text{Also } \angle C + \angle A &= 180^\circ \\ -4x + 4y + 20^\circ &= 180^\circ \\ \Rightarrow 4x - 4y &= -160^\circ \\ \Rightarrow x - y &= -40^\circ \quad \dots(ii)\end{aligned}$$

Multiplying (ii) by 3 and subtracting the result from equation (i), we get:

$$\begin{aligned}7x - 4x &= -180^\circ + 120^\circ \\ 4x &= -60^\circ \\ \Rightarrow x &= -\frac{60^\circ}{4} = -15^\circ\end{aligned}$$

Putting of $x = -15^\circ$ in equation (ii), we get:

$$\begin{aligned}-15^\circ - y &= -40^\circ \\ \Rightarrow y &= 25^\circ\end{aligned}$$

$$\therefore x = -15^\circ \text{ and } y = 25^\circ.$$

Hence,

$$\angle A = 4y + 20^\circ = 4 \times 25^\circ + 20^\circ = \mathbf{120^\circ},$$

$$\angle B = 3y - 50^\circ = 3 \times 25^\circ - 5^\circ = \mathbf{70^\circ},$$

$$\angle C = -4x = -4 \times -15^\circ = \mathbf{60^\circ}$$

$$\angle D = -7x + 5^\circ = -7 \times -15^\circ + 5^\circ = \mathbf{110^\circ}.$$